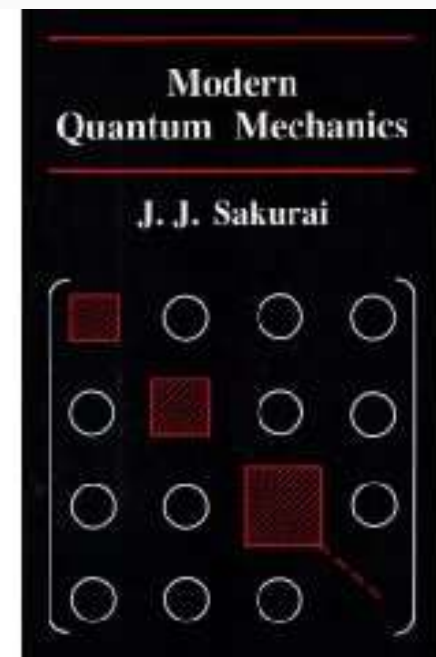
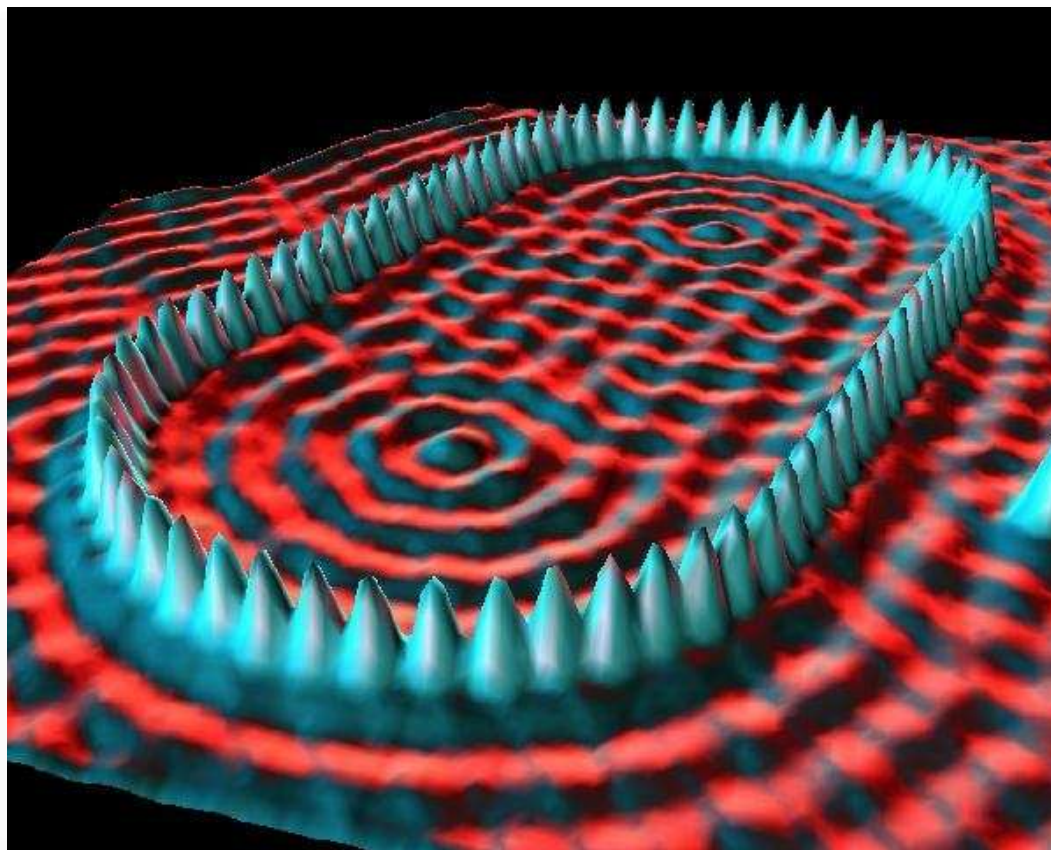


بِسْمِ اللَّهِ الرَّحْمَنِ الرَّحِيمِ

با نام و یاد خداوند متعال و با

مقدم شما دانشجو یاران محترم گرامی و شروع سال



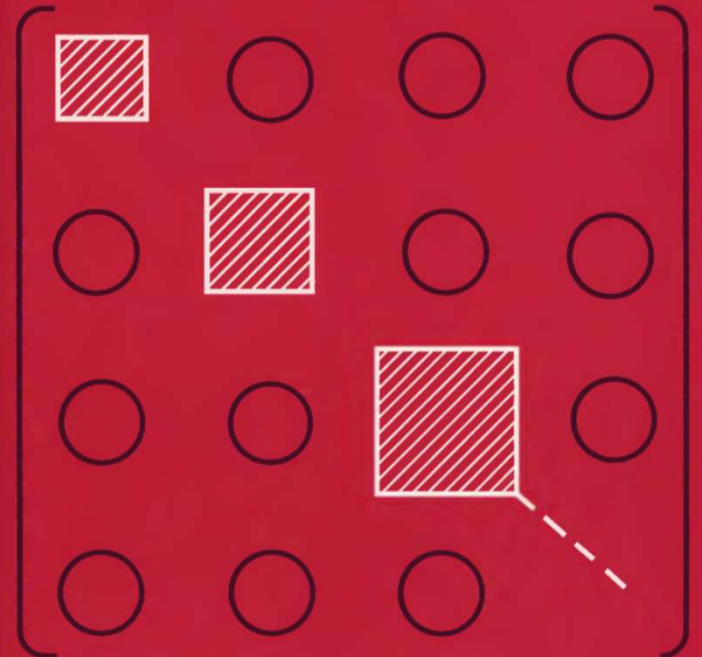
References:

- 1) J. J. Sakurai, Modern Quantum Mechanics, (1994).
- 2) Leslie E. Ballentine , Quantum Mechanics A Modern Development, (2000).
- 3) P. W. Atkins and R. S. Friedman, Molecular Quantum Mechanics, (2000).
- 4) Quantum Mechanics (2 vol. set) , Claude Cohen-Tannoudji, Bernard Diu, Frank Laloe , (1977) .
- 5) L. I. Schiff, Quantum Mechanics, (1968).
- 6) E. Merzbacher, Quantum Mechanics, (1968).
- 7) Consistent Quantum Theory, Robert B. Griffiths, (2003).
- 8) Stephen Gasiorowicz, Quantum Physics, first (1974) and third editions (2003).
- 9) J. L. Powell and B. Crasemann, Quantum Mechanics, (1961).
- 10) R. Shankar, Quantum Mechanics, (1980).

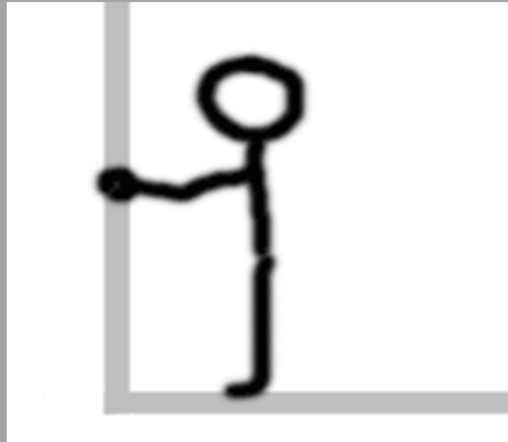
Main Reference

Modern Quantum Mechanics

J. J. Sakurai



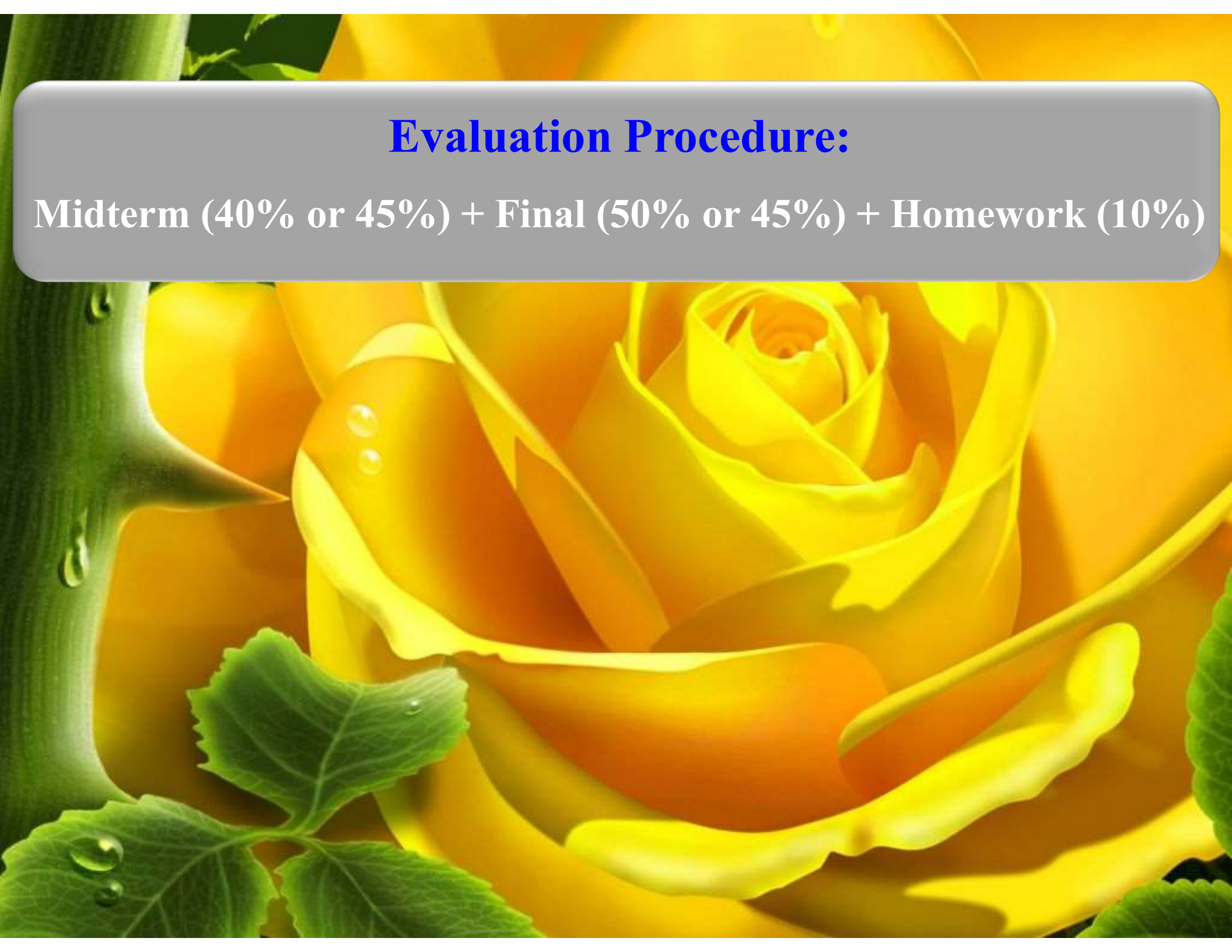
Revised Edition



Homework

You would give me your homework per week at my office
not in class or under my door.

You can work with others on homework (I encourage you to do so!),
but write it yourself.



Evaluation Procedure:

Midterm (40% or 45%) + Final (50% or 45%) + Homework (10%)

The Importance of Having Class

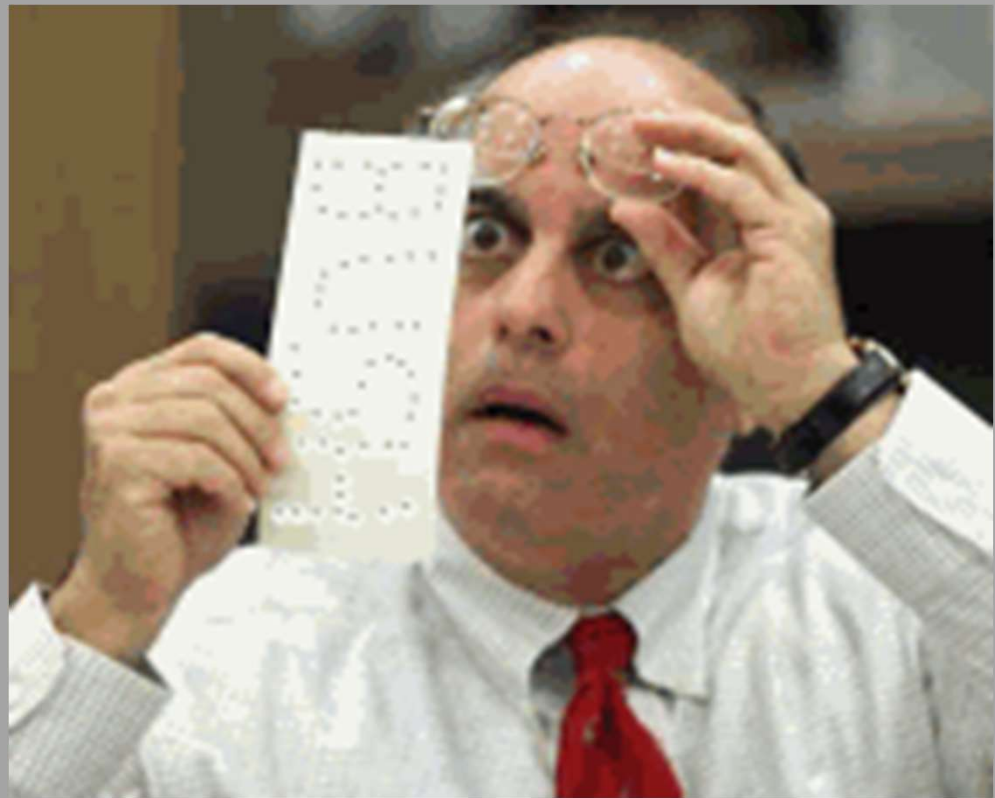
You should come to class because there's a lot that I'll say that won't be in the Power Point files. And which will be on the quizzes.

In the past, people who have skipped a lot of classes have received very bad grades. Conversely, people who've come to most or all of the classes nearly always receive good scores.



Understanding the ideas of each lecture requires the knowledge of the previous lectures.

If you keep up,
you won't end up
looking like this
the night before
the exams!

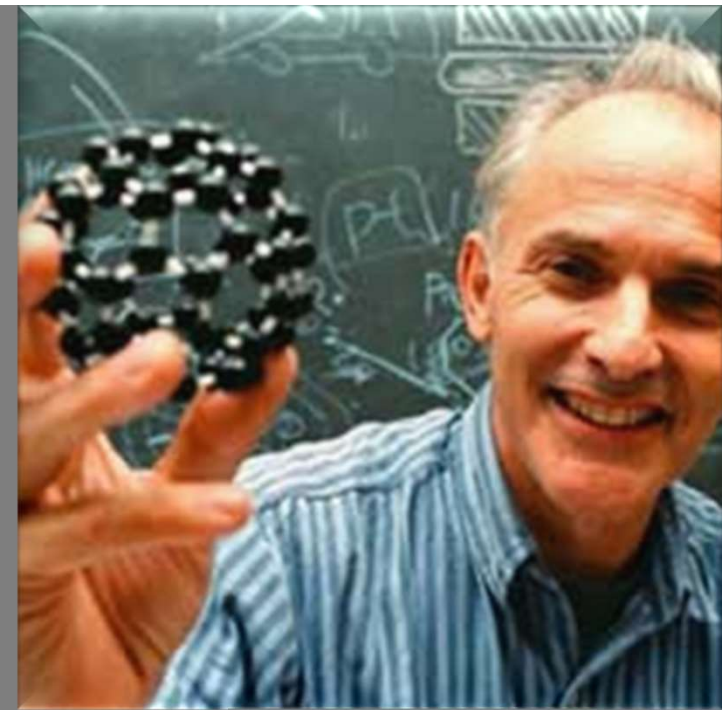




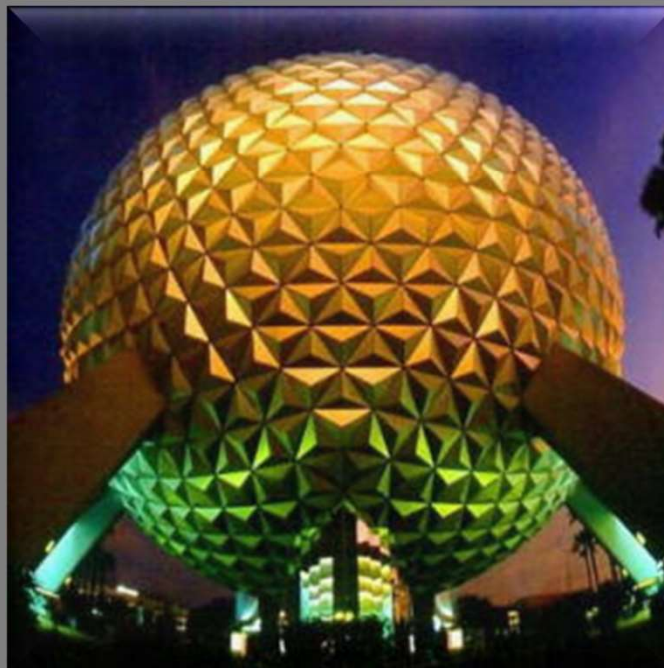
Leonardo da Vinci
1452 (Italy)-1519 (France)



Richard Buckminster Fuller
1895-1983

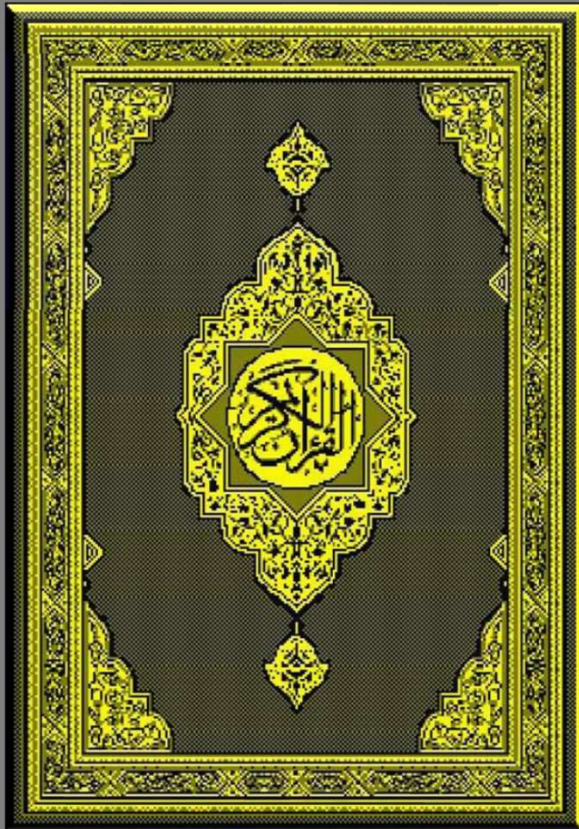


Harry Kroto, 1939



Al-Rad Sura of Quran

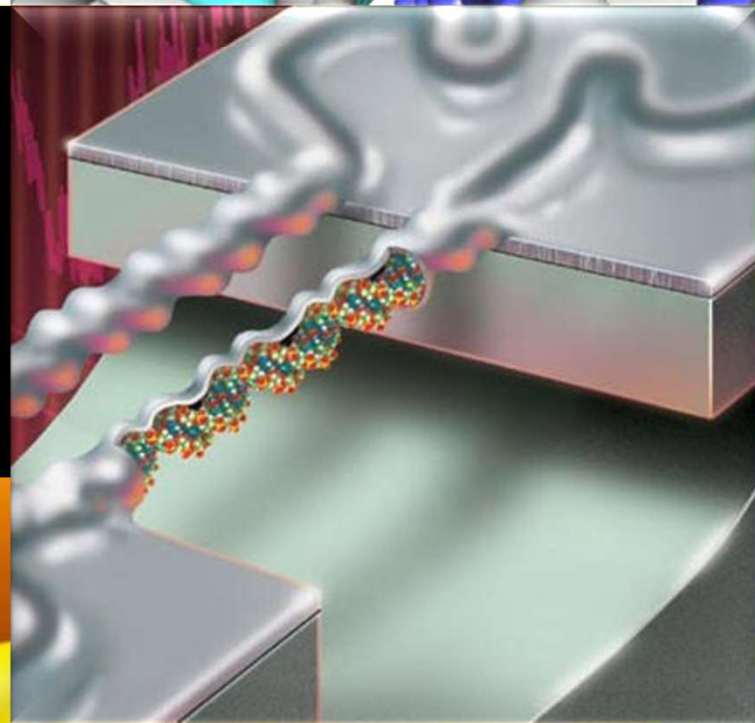
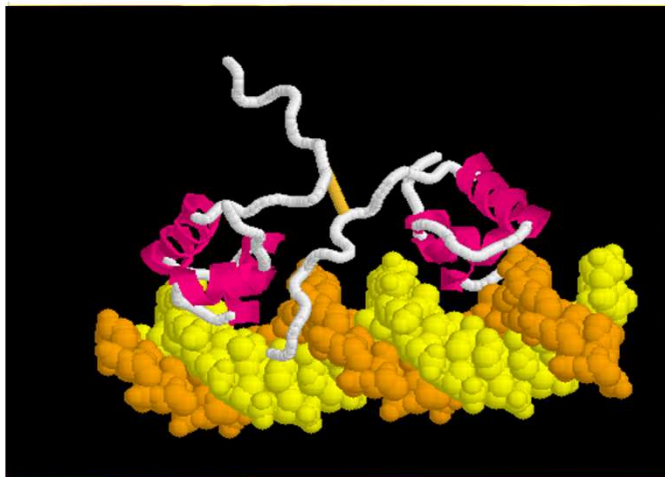
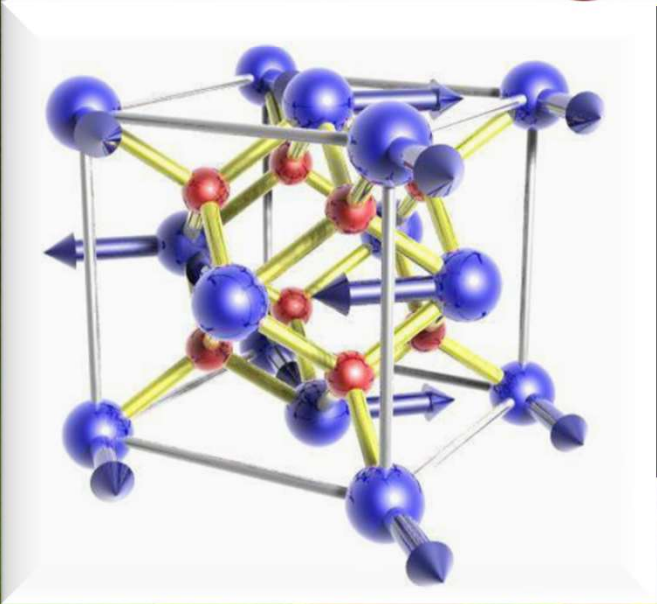
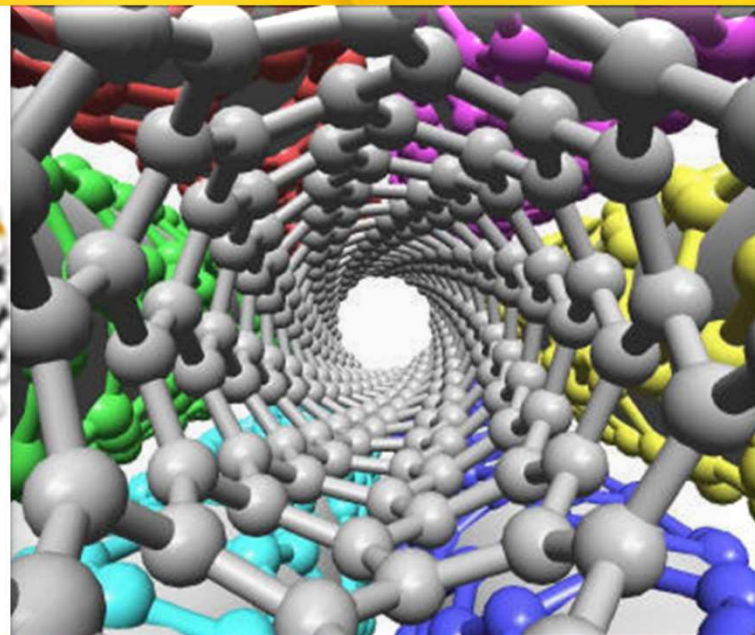
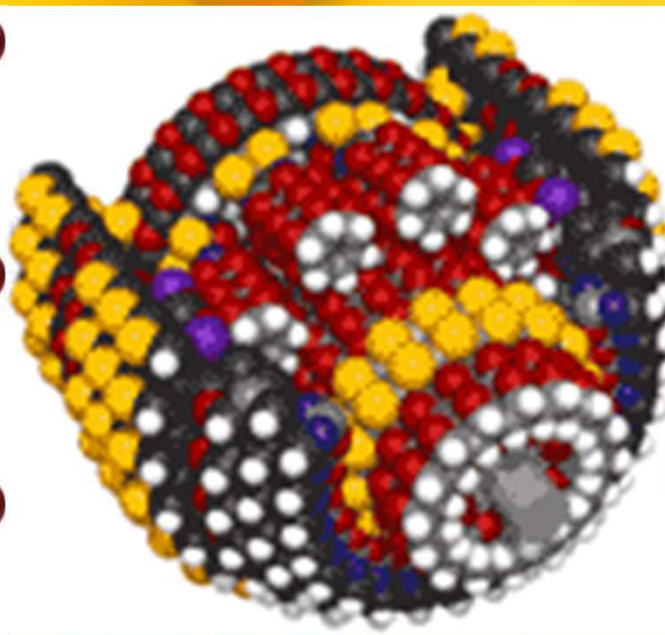
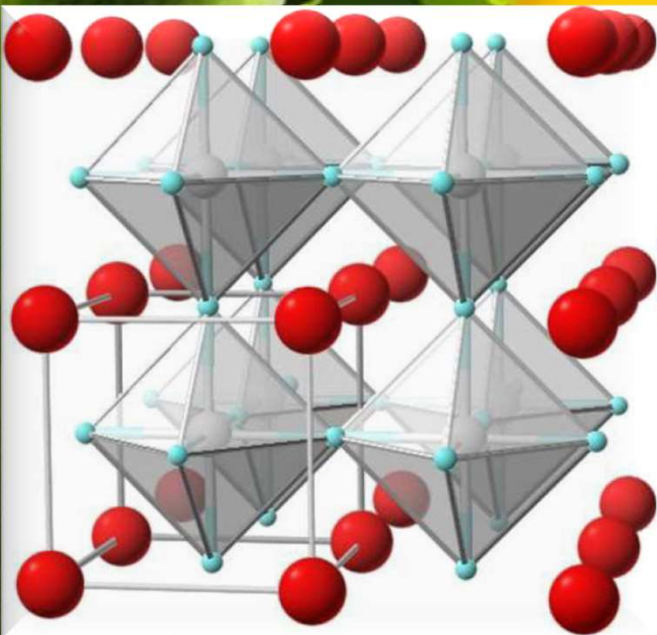
In the name of Allah, the Beneficent, the Merciful



اللَّهُ الَّذِي رَفَعَ السَّمَوَاتِ بِغَيْرِ
عَمَدٍ تَرَوْنَهَا ثُمَّ أَسْتَوَىٰ عَلَى
الْعَرْشِ وَسَخَّرَ الشَّمْسَ وَالْقَمَرَ
كُلٌّ يَجْرِي لِأَجَلٍ مُّسَمًّى يُدَبِّرُ
الْأَمْرَ يُفَصِّلُ الْآيَاتِ لَعَلَّكُمْ
بِلِقَاءِ رَبِّكُمْ تُوقِنُونَ (2)



Allah it is who raised up the universe without visible supports, then mounted the Throne, and compelled the sun and the moon to be of service, each runneth unto an appointed term; He ordereth the course; He detaileth the revelations, that haply ye may be certain of the meeting with your Lord. (2)

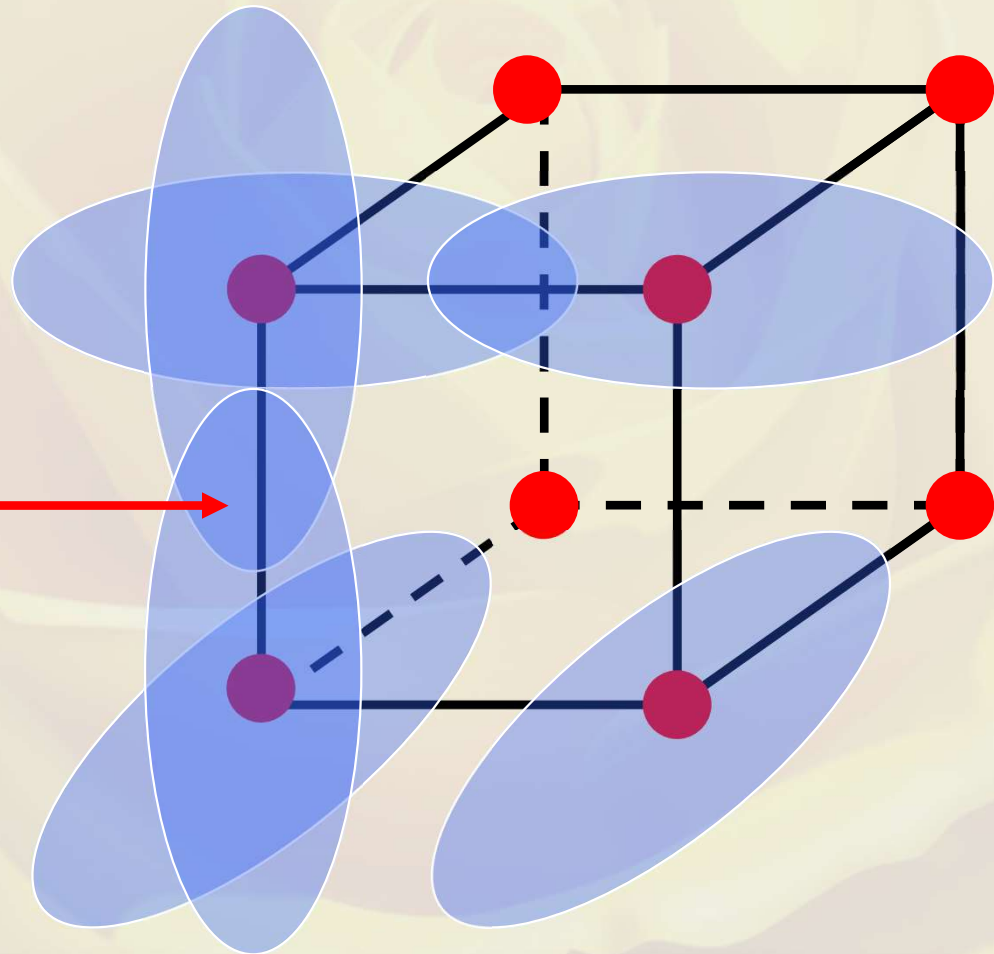


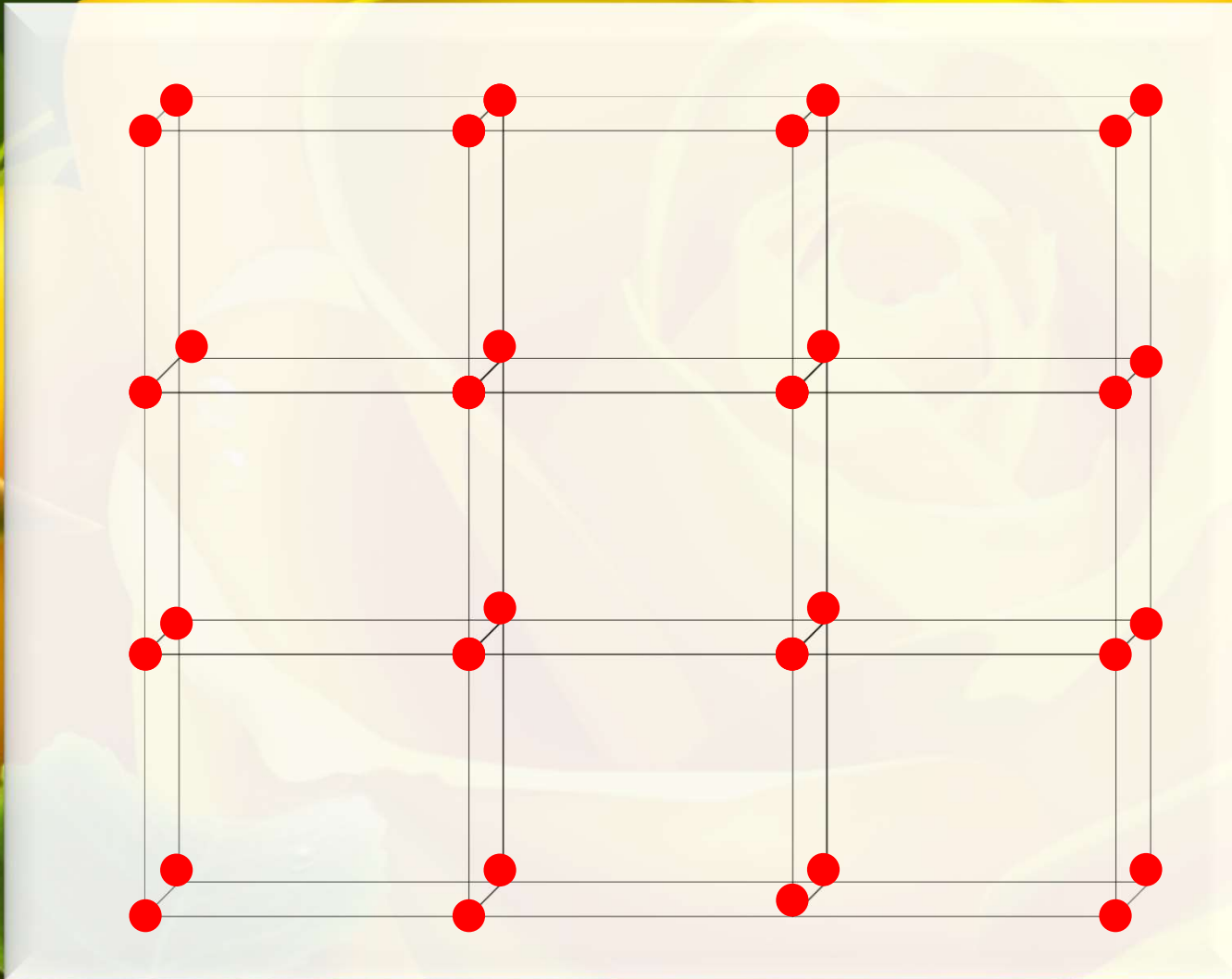
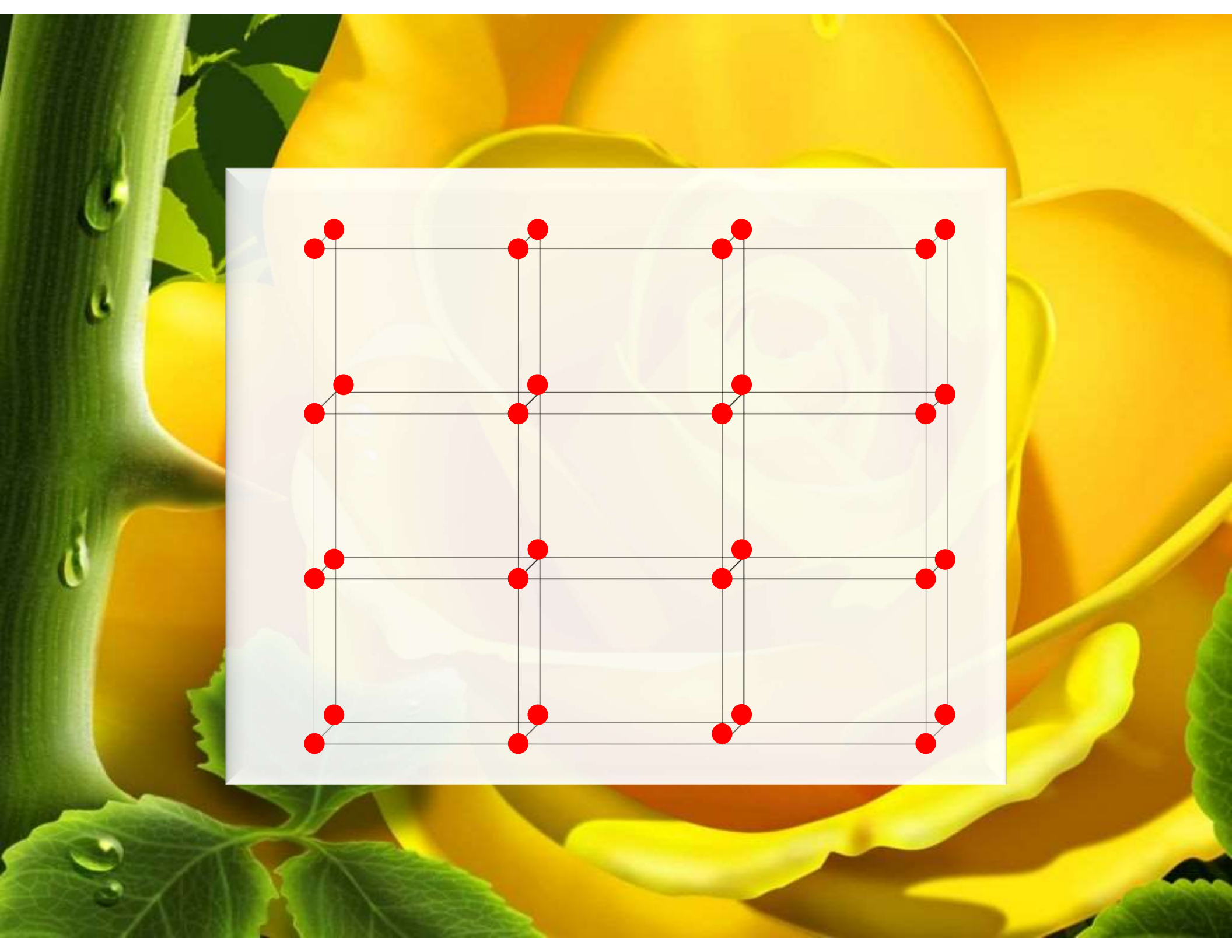


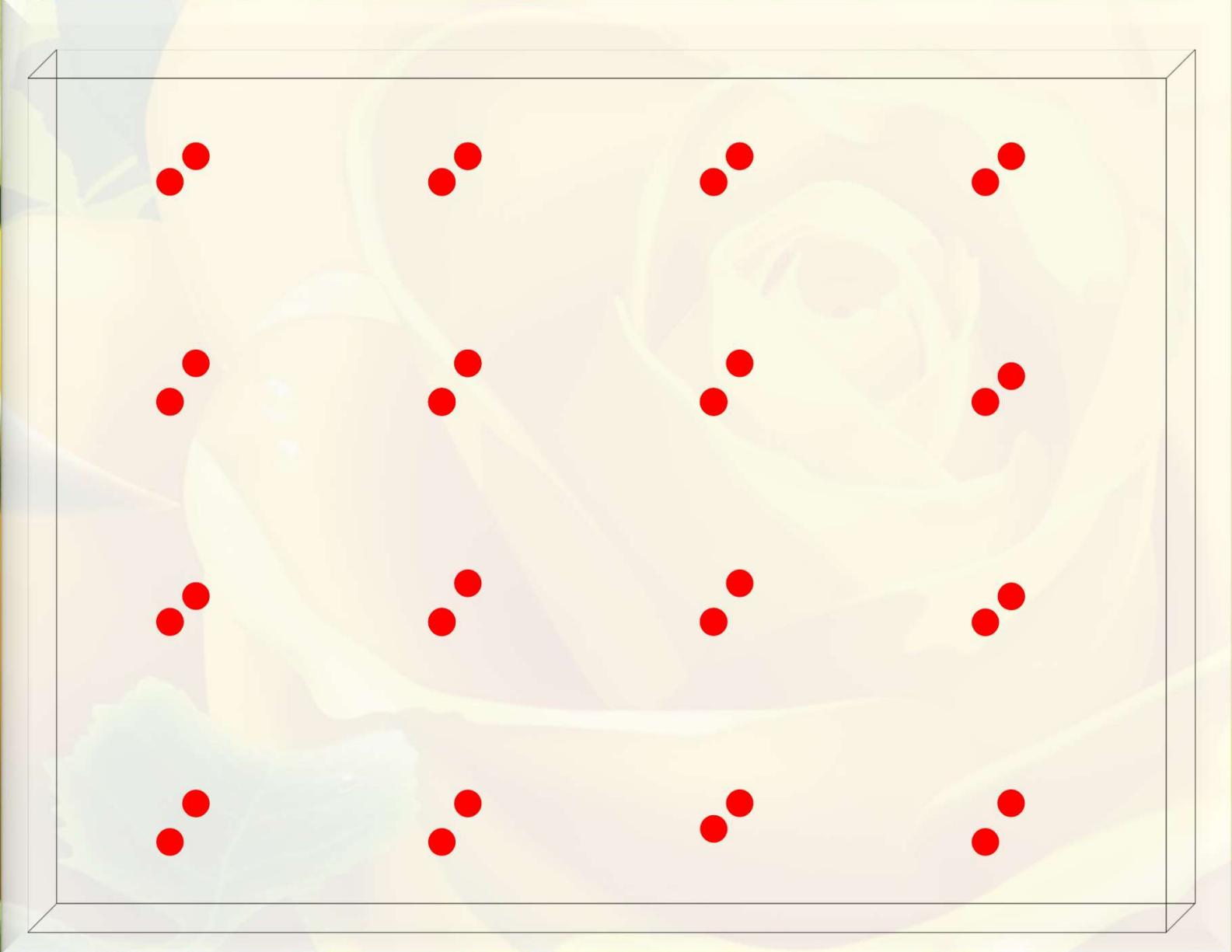
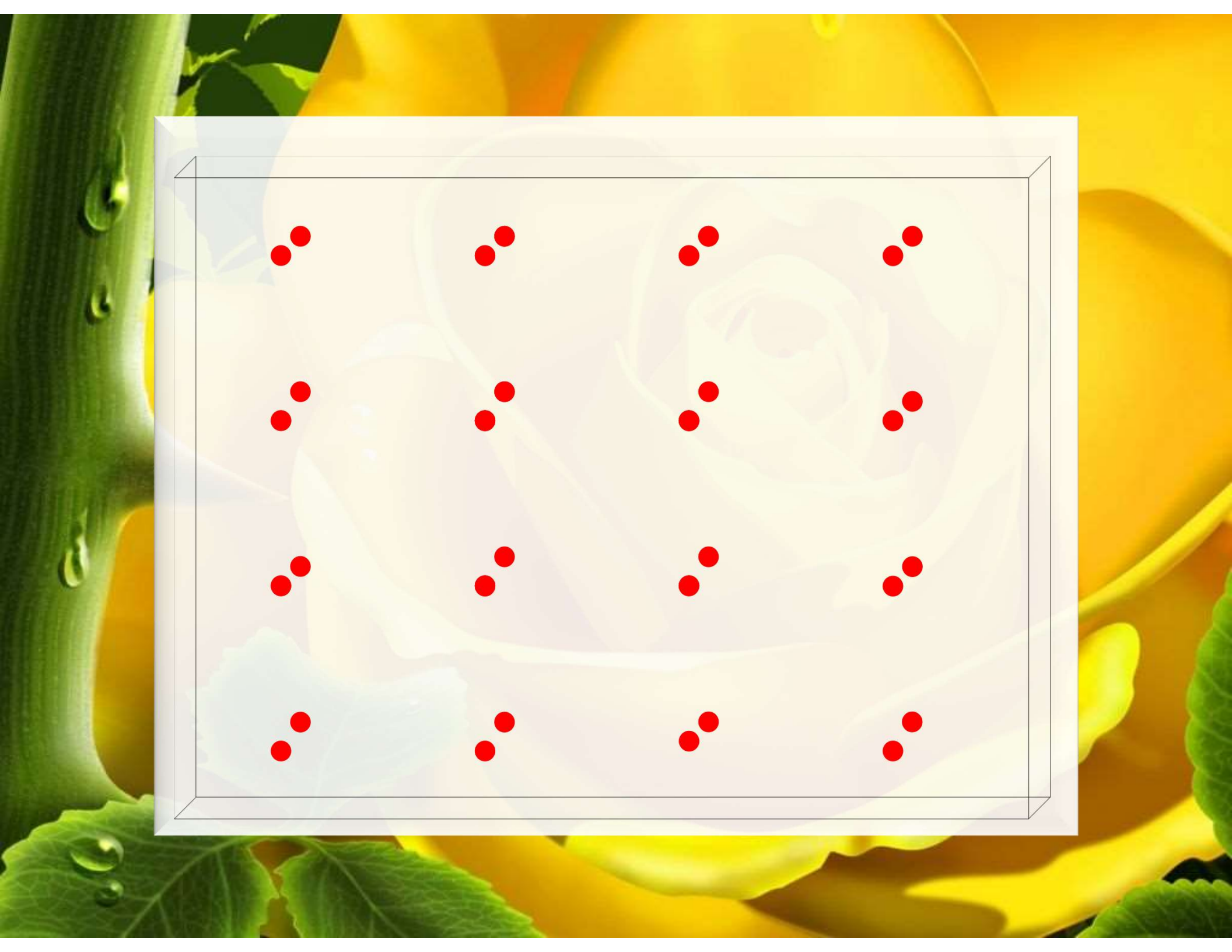
The classical ideal gas

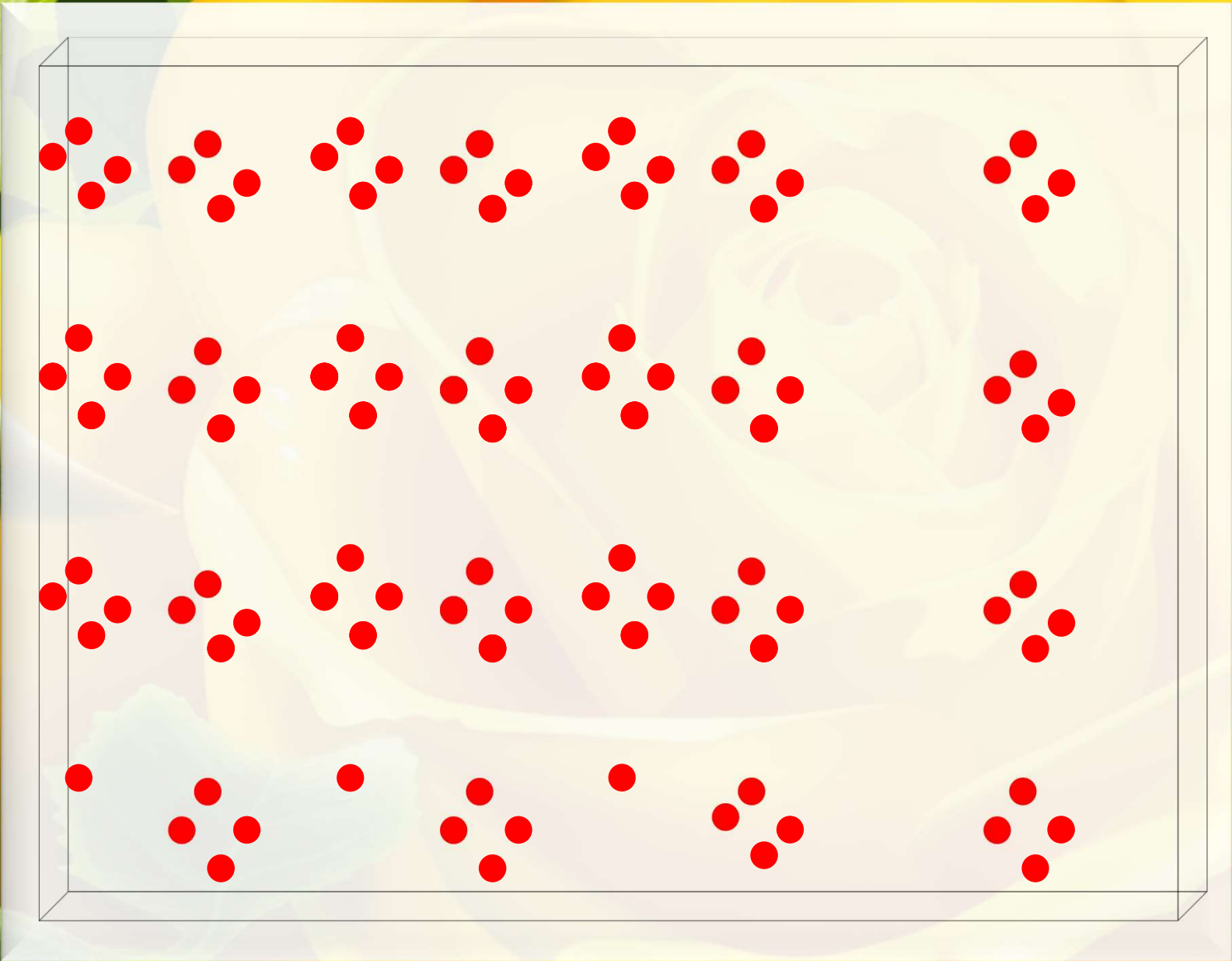
$$H\Psi = E\Psi$$

$$H = T + V \longrightarrow$$







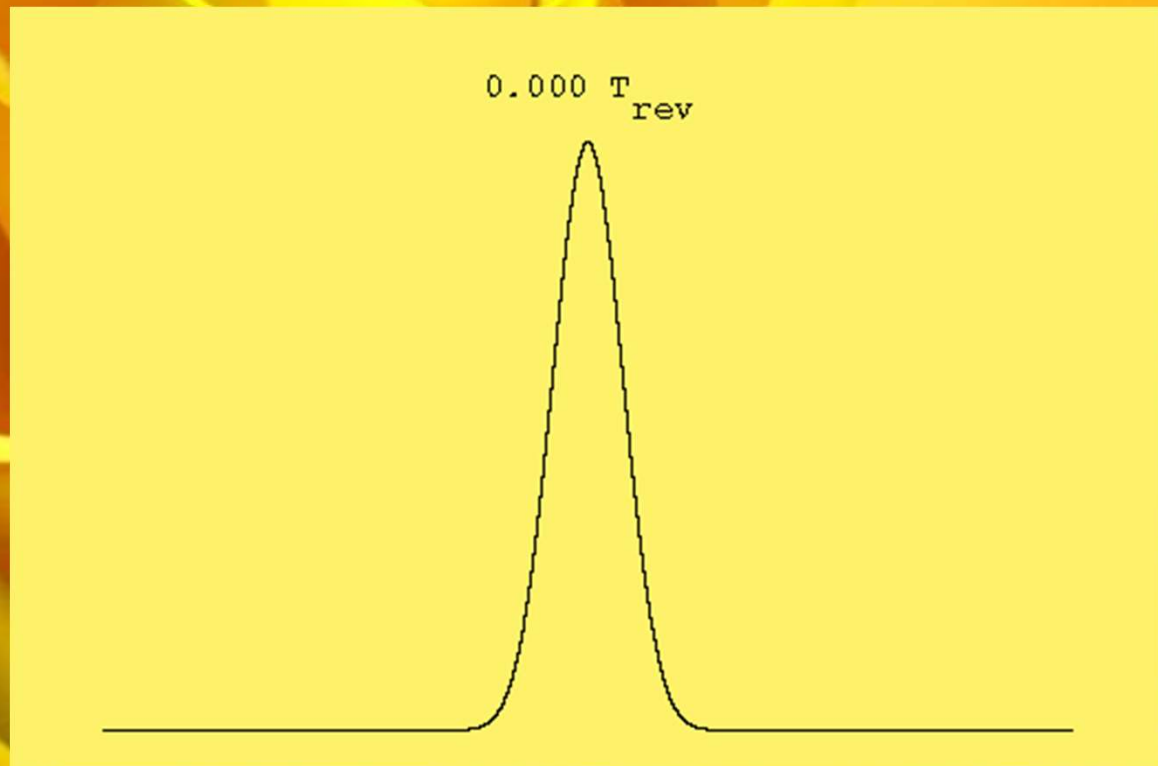
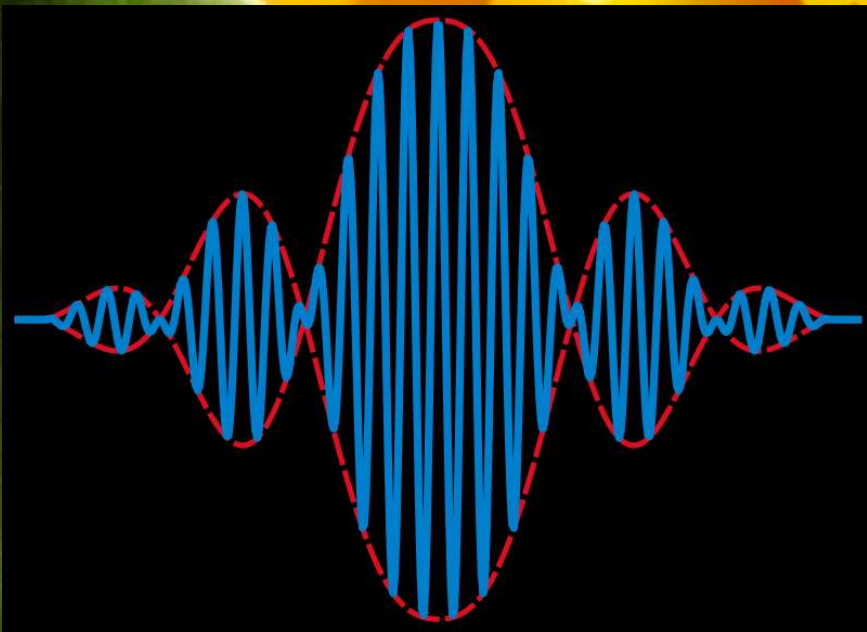


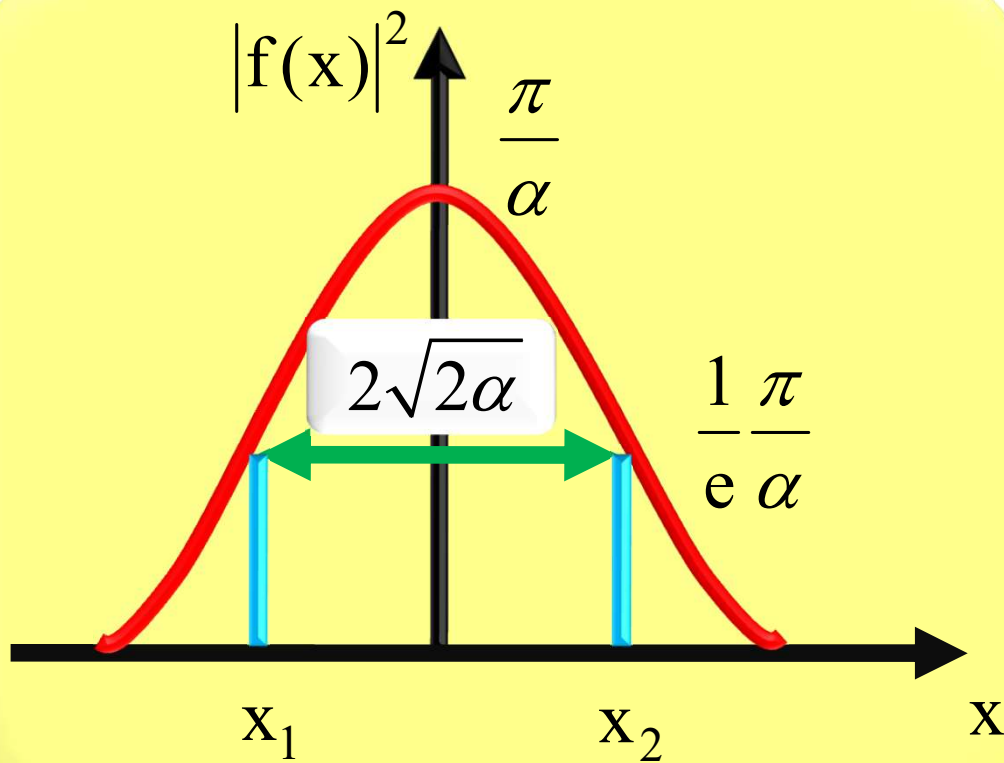


Tsunami

Theoretical Tools to Study Wave Packet

$$f(x) = \int_{-\infty}^{\infty} dk g(k) e^{ikx}$$

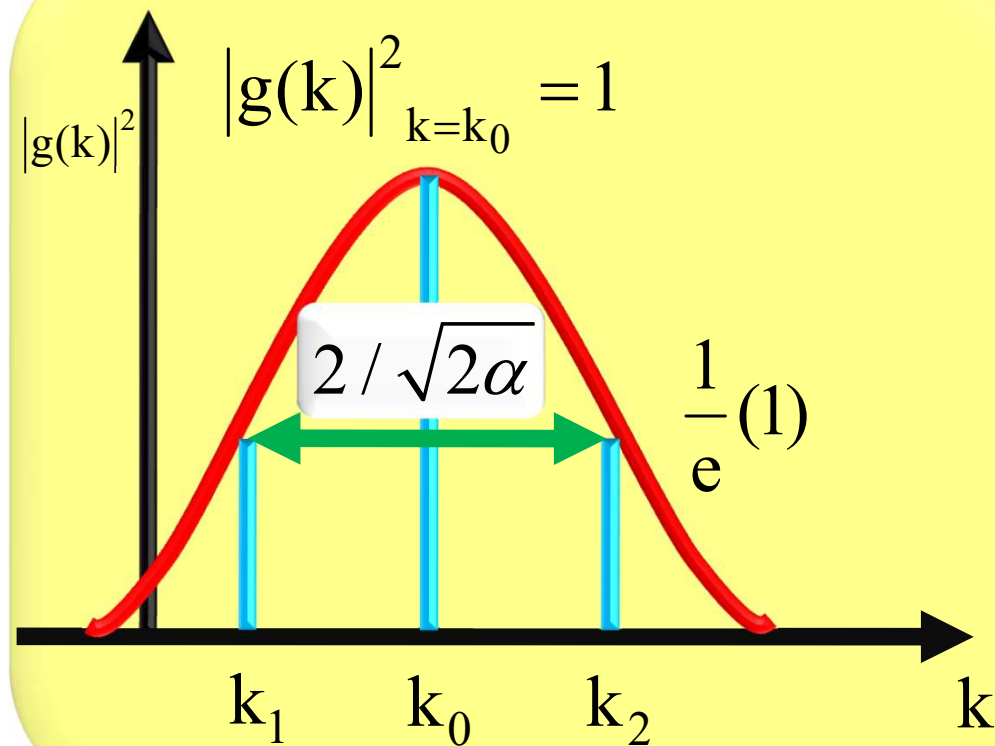




$$\Delta x = x_2 - x_1 = 2\sqrt{2\alpha}$$

Larger alpha results in larger width
This gives rise to wider function.

Smaller alpha results in smaller width
This gives rise to more localized function.



$$k_2 - k_1 = \Delta k = 2/\sqrt{2\alpha}$$

Larger alpha results in smaller width
This gives rise to thinner function.

Smaller alpha results in larger width
This gives rise to more itinerant function.

$$\Delta x = x_2 - x_1 = 2\sqrt{2\alpha}$$

$$k_2 - k_1 = \Delta k = 2/\sqrt{2\alpha}$$

$$\Delta k \Delta x = (2/\sqrt{2\alpha})(2\sqrt{2\alpha}) = 4$$

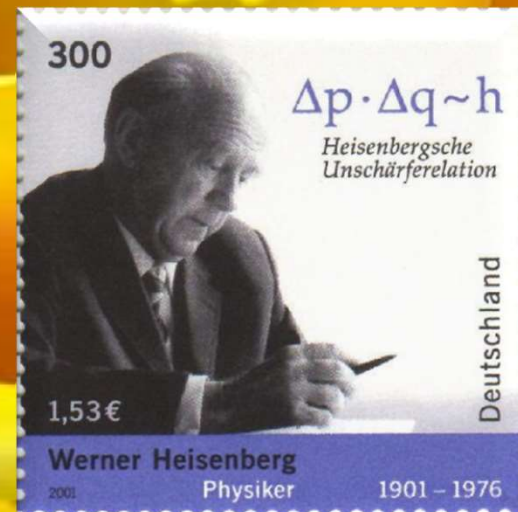
$$\Delta k \Delta x = 4$$

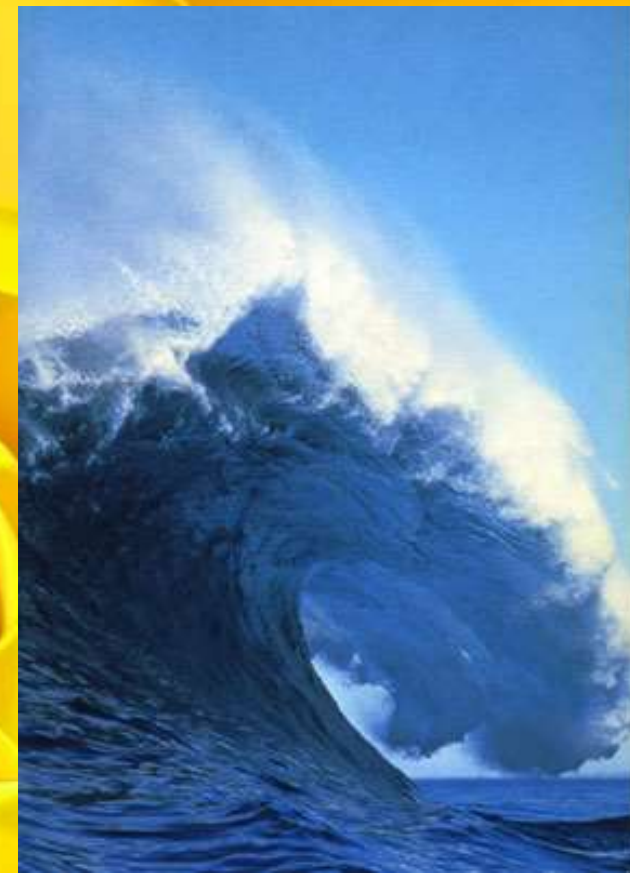
Wave vector k space behaves as inverse (reciprocal) of real x space.

$$\Delta k \Delta x \geq O(1)$$

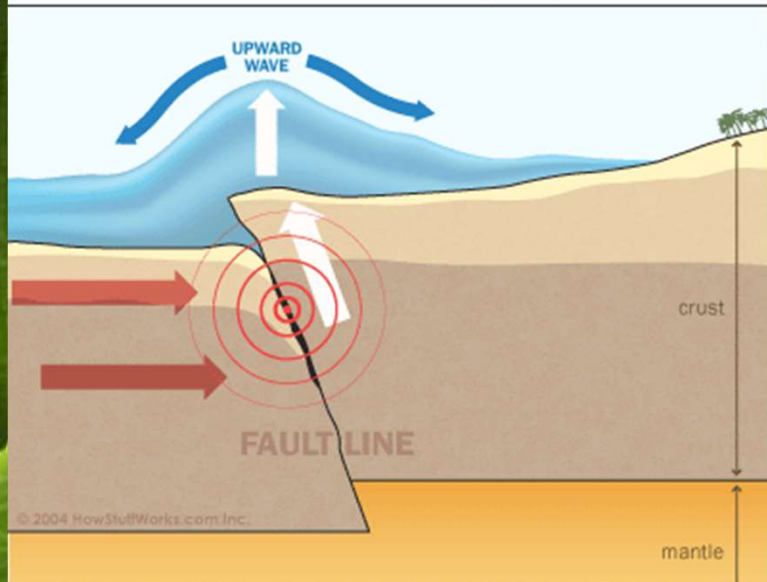


This is independent of alpha. It is a general characteristic of wave packets. But we will soon see that this fact refers to a deep aspect in quantum mechanics.

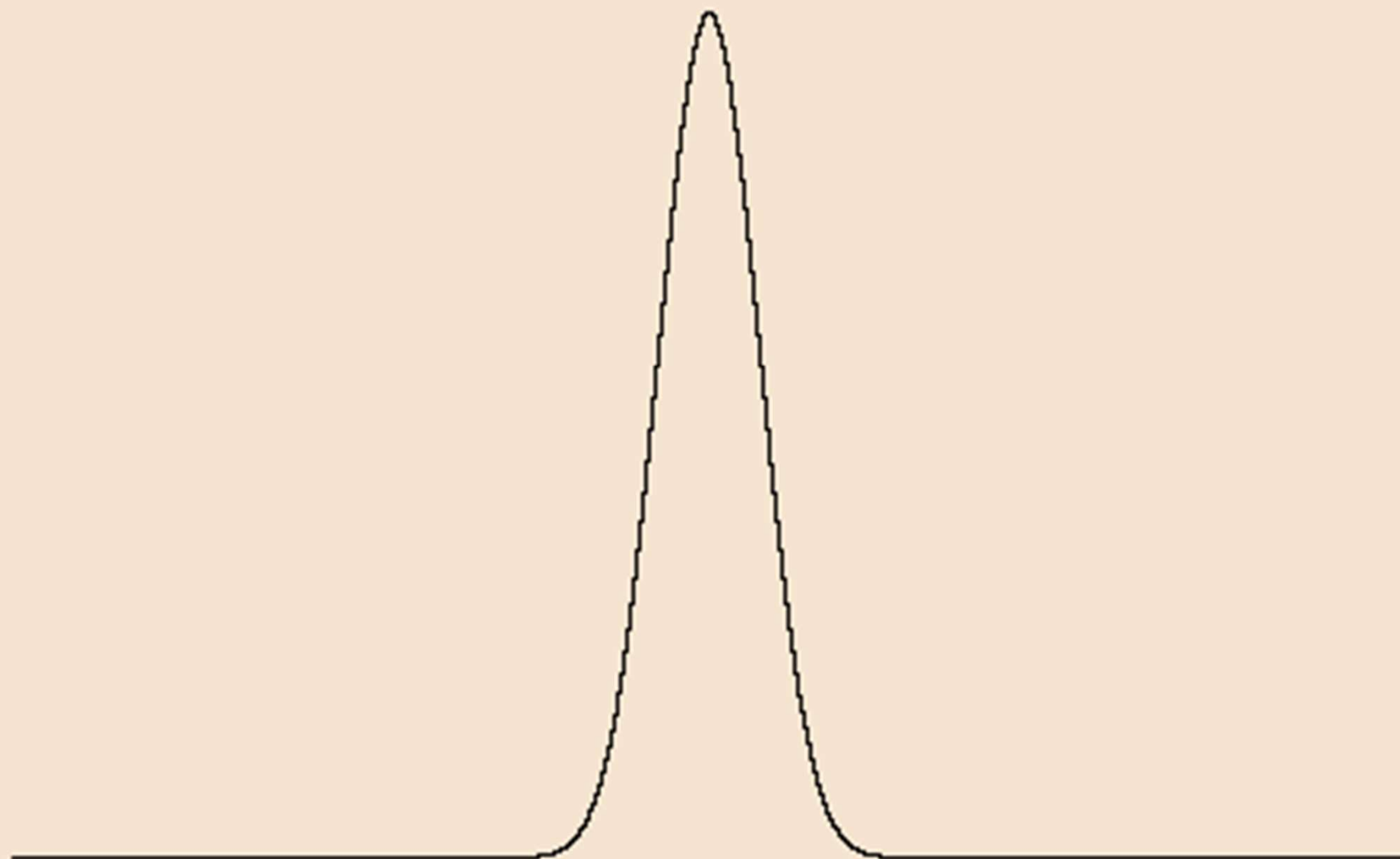


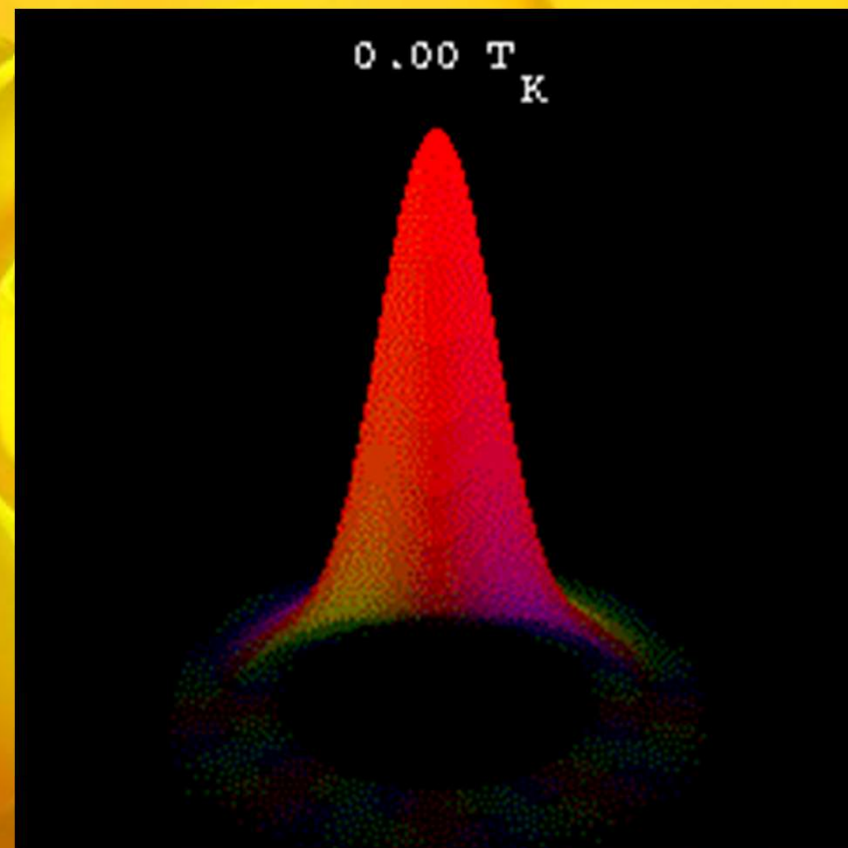
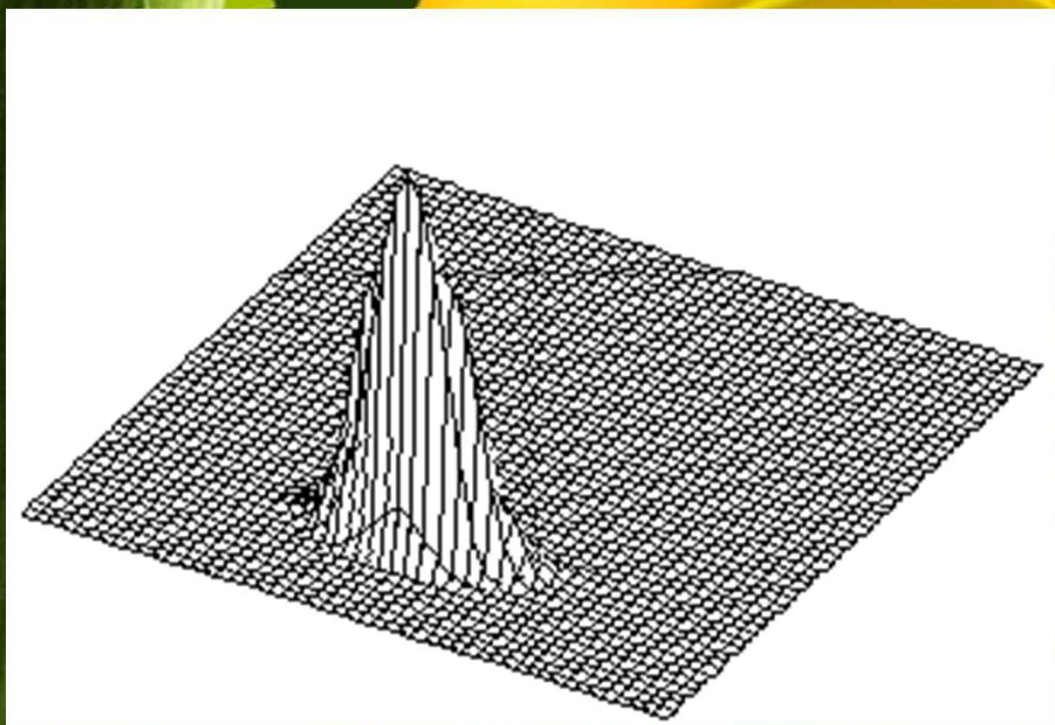


How Tsunamis Work: Tsunamigenesis

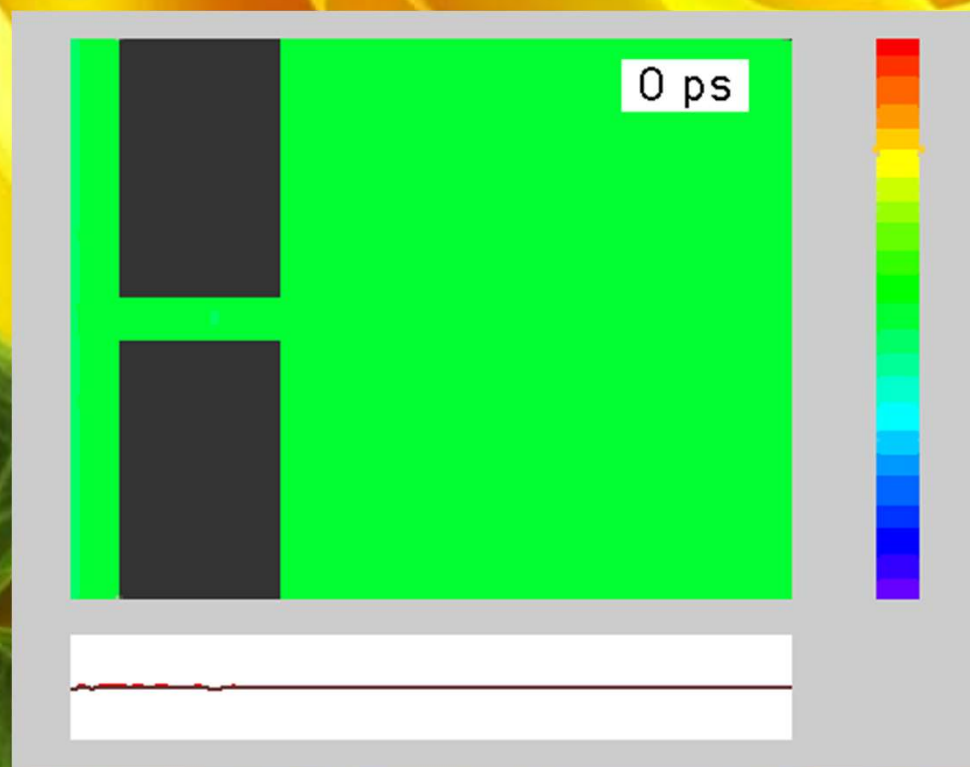


0.000 T_{rev}













The revolutions in physics inspired revolutions in other fields, too.

Fields like chemistry, engineering, and biology necessarily also underwent revolutions because physics is their basis.

And mathematics also began to see flaws in its fundamental foundations.

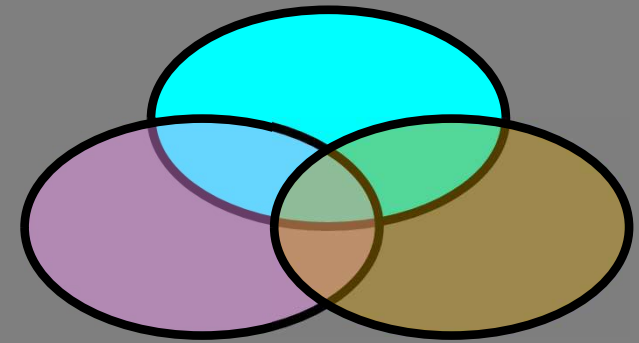
And the revolutions in physics spurred revolutions in art, music, architecture, and psychology and even changed the way the average person saw the world.



Bertrand Russell
(1872-1970)

http://en.wikipedia.org/wiki/Bertrand_Russell

Weirdness in mathematics: Russell's Paradox (1901)



Consider a set that contains itself.

Example: $\{ \{\}, \{ \{\}, \{\{\}\} \}, \dots \}$

Next consider the set of all sets that contain themselves.

Now consider **the set of all sets that don't contain themselves**.

Does this last set contain itself?

If it doesn't, then it does. But if it does, then it doesn't.

Because set theory is the basis of all mathematics (and numbers!), this fundamental paradox is a serious crack in the foundations of mathematics.

Russell's Paradox

© Copyright 2000, Jim Loy

Let you tell me a famous story:

There was once a barber. Some say that he lived in Seville. Wherever he lived, all of the men in this town either shaved themselves or were shaved by the barber. And the barber only shaved the men who did not shave themselves.

That is a nice story. But it raises the question: **Did the barber shave himself?** Let's say that he did shave himself. But we see from the story that he shaved only the men in town who did not shave themselves. Therefore, he did not shave himself. But we again see in the story that every man in town either shaved himself or was shaved by the barber. So he did shave himself. We have a contradiction. What does that mean?

Maybe it means that the barber lived outside of town. That would be a loophole, except that the story says that he did live in the town, maybe in Seville. Maybe it means that the barber was a woman. Another loophole, except that the story calls the barber "he." So that doesn't work. Maybe there were men who neither shaved themselves nor were shaved by the barber. Nope, the story says, "All of the men in this town either shaved themselves or were shaved by the barber." Maybe there were men who shaved themselves **AND** were shaved by the barber. After all, "either ... or" is a little ambiguous. But the story goes on to say, "The barber only shaved the men who did not shave themselves." So that doesn't work either. Often, when the above story is told, one of these last two loopholes is left open. So I had to be careful, when I wrote down the story.

More weirdness in Mathematics: Gödel's Incompleteness Theorem (1931)

In 1931, Kurt Gödel proved that there are **theorems that can neither be proven nor disproven**.

This solved the second of David Hilbert's famous list of the 23 most important unsolved math problems.

And Hilbert's first problem turned out to be one of Gödel's unprovable theorems ("the continuum hypothesis"—whether there's an infinity between the number of integers, $\aleph_0$, and the number of real numbers, $\aleph_1$)!



Kurt Gödel (1906 – 1972)

Weirdness in Art

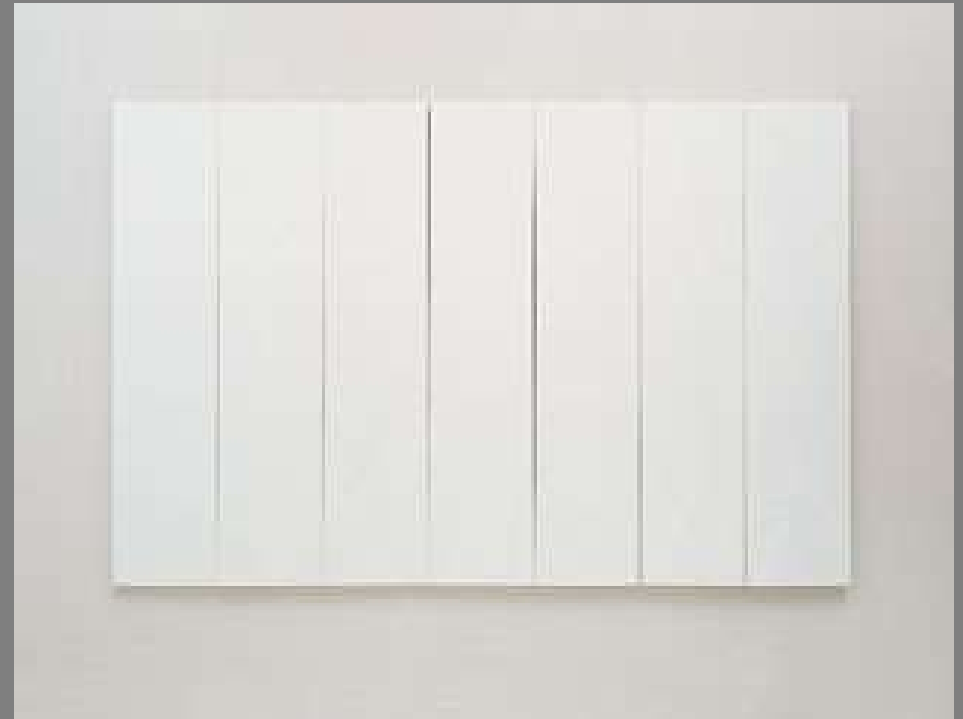
Whereas pre-20th-century art was very literal, modern art has become very abstract and unintuitive.

Pre-1905 art



The Death of Socrates (1787)
Jacques-Louis David

Post-1905 art



White Painting (1951)
Robert Rauschenberg

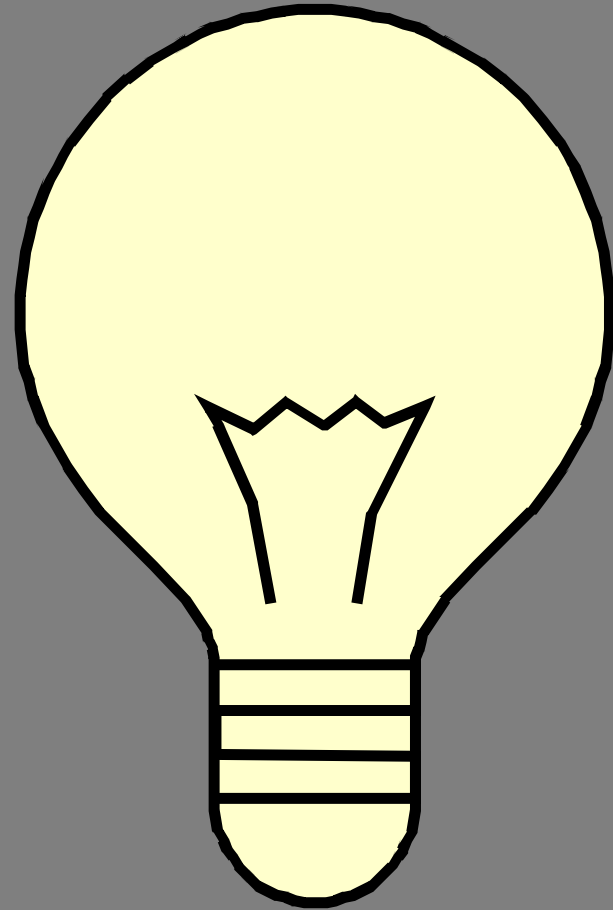
Interestingly, most “great” works of modern art have only required a few minutes of effort to create.

Modern art is getting weirder and weirder.

“Light in [an empty] room turning on and off” won the top British art prize (The Turner Prize, £20,000) in 2001.



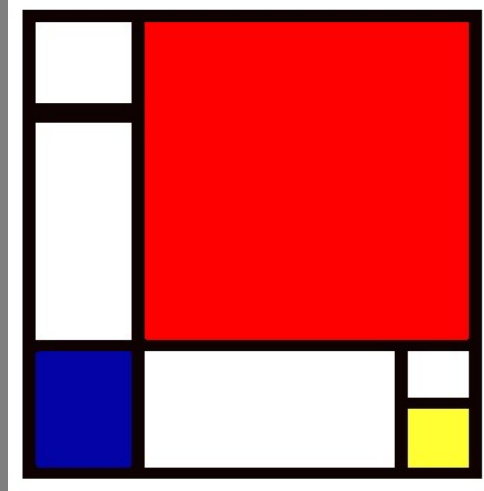
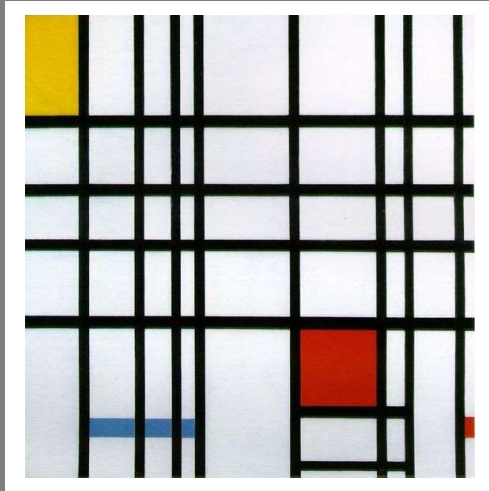
Martin Creed
Winner of prize



And this is one of the least objectionable and ridiculous winners of this prize.

Weirdness in Art Appreciation

Pieter
Mondrian
1872 - 1944



Mondrian's art “was, in the end, to be so fine that, having induced a radiant harmony and balance throughout society, the need for painting itself would no longer be necessary.”

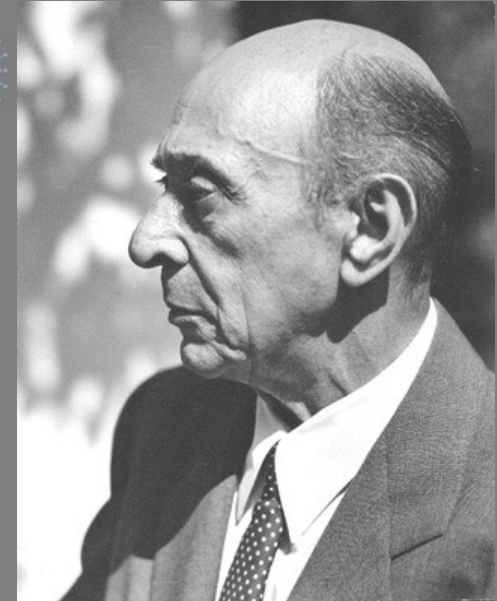
Bennett Schiff, *Smithsonian* 1995

Mondrian died in 1944, a time of complete radiant harmony and balance throughout society...

Weirdness in Music



In 1907 Schoenberg, who stated publicly that he wanted to do for music what Einstein did for physics, introduced **atonal music**, which violated all known principles of what constituted good music and, for the most part, sounds like noise.



Arnold Schoenberg (1874 - 1951)

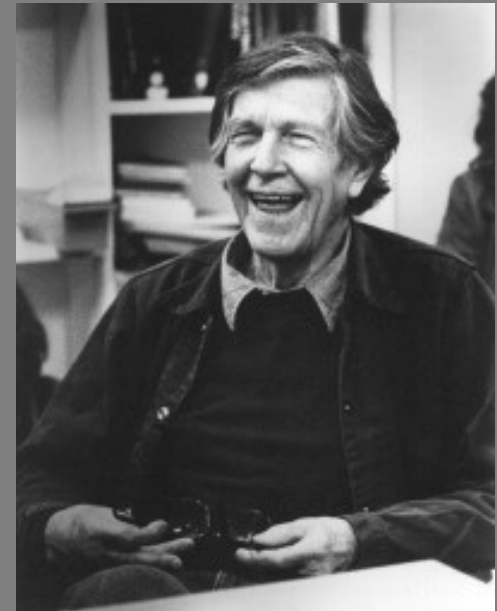


Stephen Reich (1936 -)



John Cage
(1912 - 1992)

John Cage is best known for his 1952 composition, 4'33", whose three movements are each composed entirely of silence.

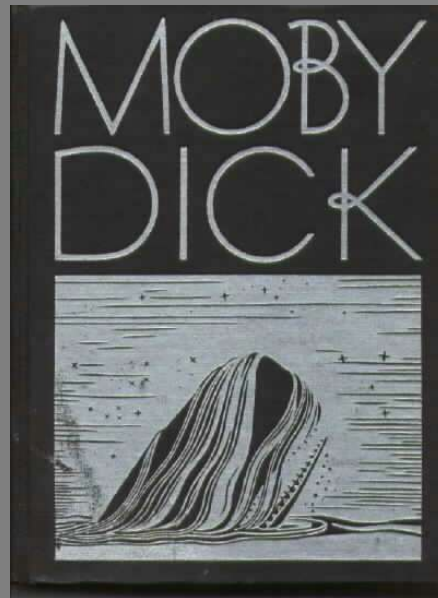


Weirdness in Literature

19th century literature:

“Call me Ishmael...”

Herman Melville's *Moby Dick* (1851) was first and foremost a simple whaling story, but it was also a superb study of human obsession and taught us about human nature.



20th century literature:

“...Throgmoggle Fordful
mantly overgoo
bog manty gong goppling
rill cum nack throgginds.

Choomin:

Chillchincar Engestchin
chanty chopcharchill
chorey chopcharchill chooley
chingle choon chingley
choodle.

Throgmoggle Fordful?

Chillchincar Engestchin?

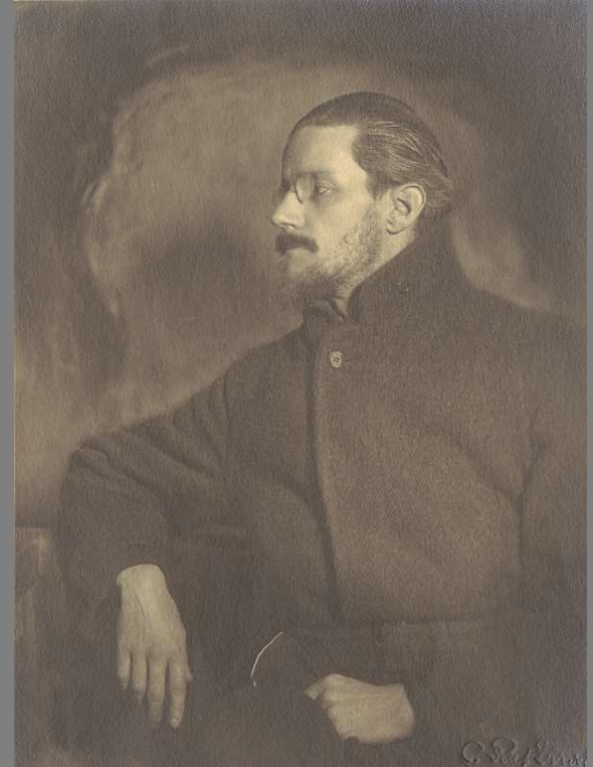
Fulford mog-gle throg

Throggins...”

Colleen Thibaudeau's
*From Throgmoggle &
Engestchin: A relationship*
(1991)

20th Century Literature

John Bishop, in his introduction to James Joyce's *Finnegans Wake* in 1999, wrote these less-than-encouraging words: "There is no agreement as to what *Finnegans Wake* is about, whether or not it is 'about' anything, or even whether it is, in any ordinary sense of the word, 'readable.' Since Joyce's sentences are packed with obscure allusions, often written in dozens of different languages, it remains impossible to compile a definite synopsis of *Finnegans Wake*."



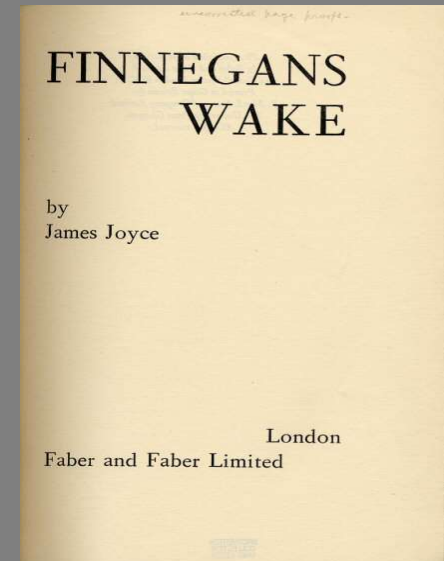
James Joyce
1882 - 1941

Literary critic Fritz Senn said of the currently available summaries: "We have some traditional summaries, some by Joyce himself. I find them most unsatisfactory and unhelpful..."

Excerpt from *Finnegans Wake*

You're probably thinking that I'm exaggerating.

Here's an excerpt (chosen at random) from this "classic" of modern literature:



“...The fall (bababadalgharaghtakamminarronnkonnbronntonner-ronntuonnthunntrovarrhounawnskawntooohooordenenthur-nuk!) of a once wallstrait oldparr is retaled early in bed and later on life down through all christian minstrelsy. The great fall of the offwall entailed at such short notice the pftjschute of Finnegan, erse solid man, that the humptyhillhead of himself promptly sends an unquiring one well to the west in quest of his tumptytumtoes: and their upturnpikepointandplace is at the knock out in the park where oranges have been laid to rust upon the green since dev-linsfirst loved livvy. ...”

Weirdness in Sculpture, and Architecture

The architect himself says his \$300 million new computer science and artificial intelligence building at M.I.T. “looks like a party of drunken robots got together.”





Sigmund Freud
(1856 – 1939)

Weirdness in Psychology

Sigmund Freud (and others) developed a bizarre and complex theory of human behavior—psychoanalysis—based mostly on sexual desire.

Psychoanalysis is **unfalsifiable**. If you deny your Oedipal complex, then you're repressing it!

Richard Webster called psychoanalysis “one of the great follies of Western civilization.”

H. J. Eysenck says that Freud “set psychiatry back 100 years,” consistently misdiagnosed his patients, fraudulently misrepresented case histories, and that “what is true in Freud is not new, and what is new in Freud is not true.”

J. von Scheidt speculated that Freud's theories were due to his cocaine use, which increases sexual interest and obsessive thinking.

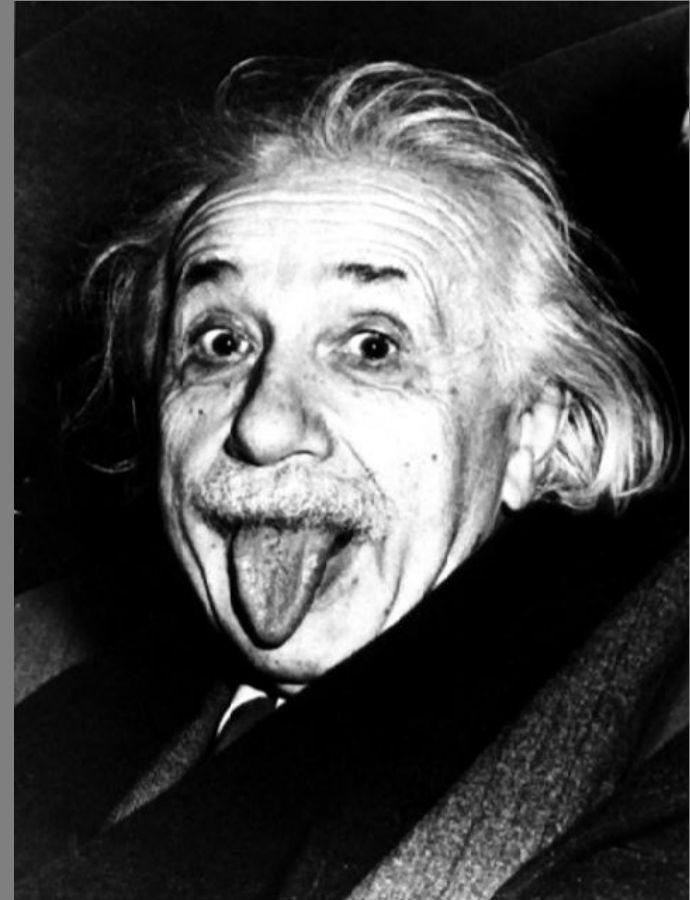
In any case, Freud was clearly **subconsciously** influenced by physics!

Genuine vs. Artificial Revolutions

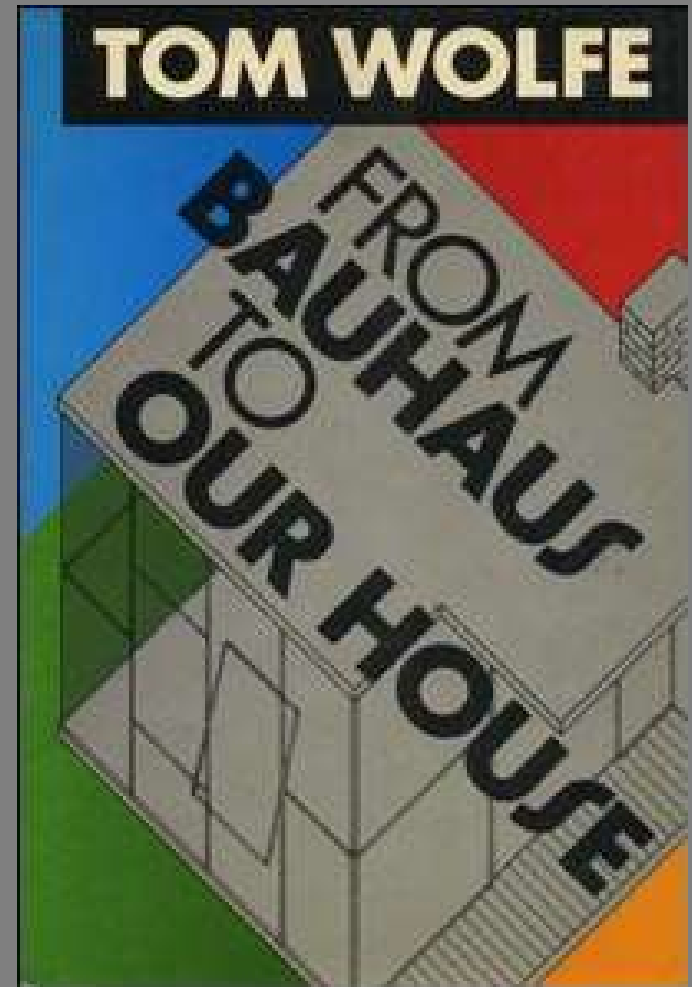
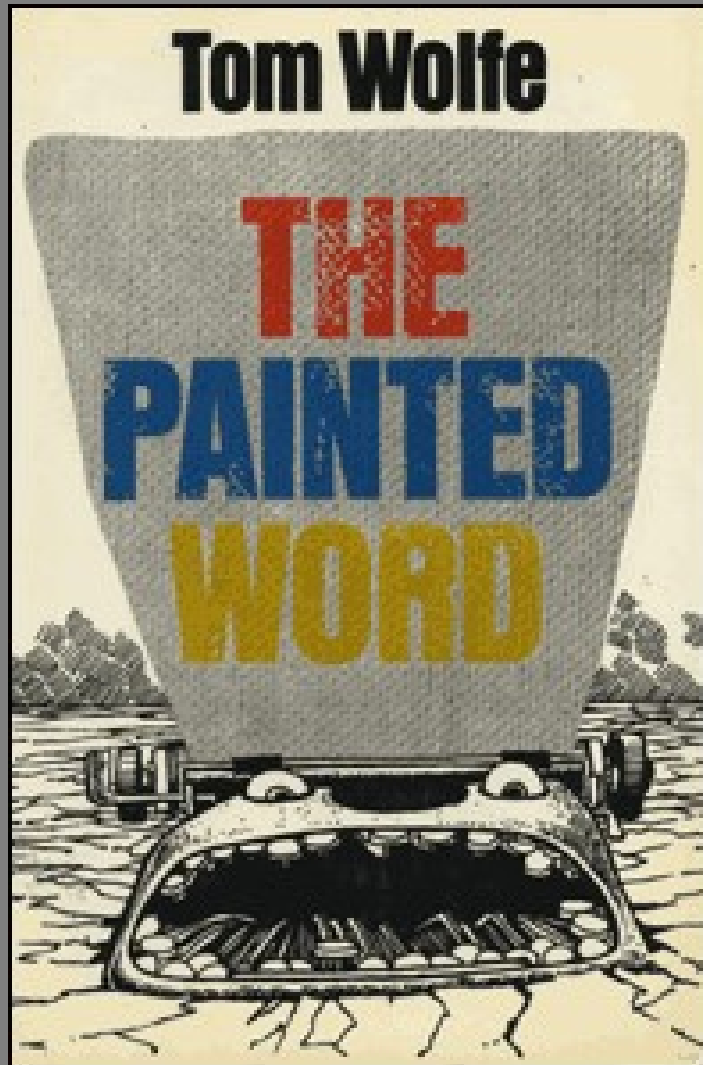
The revolutions in physics were the result of new **experiments** and **observations** and so were **forced** upon us by the world around us.

That they involved weird ideas that average people couldn't understand is due to the fact that the universe is, in fact, weird.

The “revolutions” in art, literature, psychology, and music were the result of simple arrogance of the practitioners and their desire to have their own unintuitive ideas that only they could “understand”—what I like to call **Physics Envy**. But they nicely illustrate the dramatic effects on others of the genuine revolutions that occurred in physics.



To read more about weirdness in modern art and architecture...



Artists and architects
hate these two books...

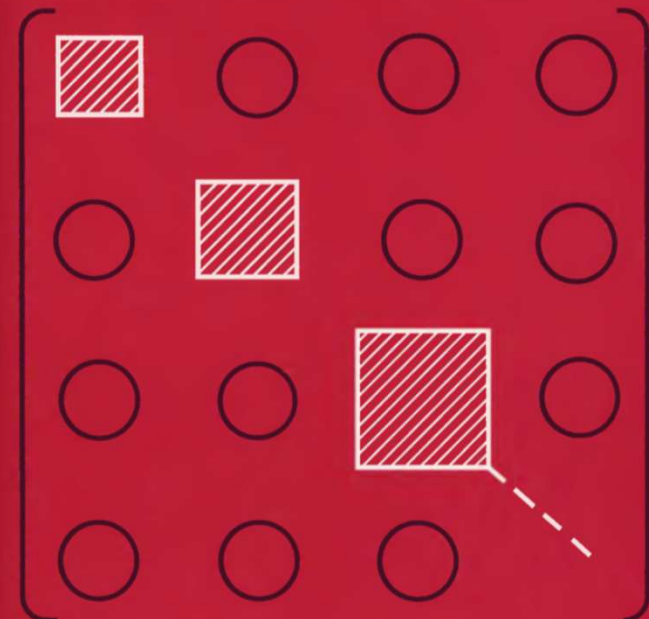
Modern Quantum Mechanics



J. J. Sakurai (1933-1982)

Modern Quantum Mechanics

J. J. Sakurai



Revised Edition

What we will learn

Modern Quantum Mechanics I

1) FUNDAMENTAL CONCEPTS

2) QUANTUM DYNAMICS

3) THEORY OF ANGULAR MOMENTUM

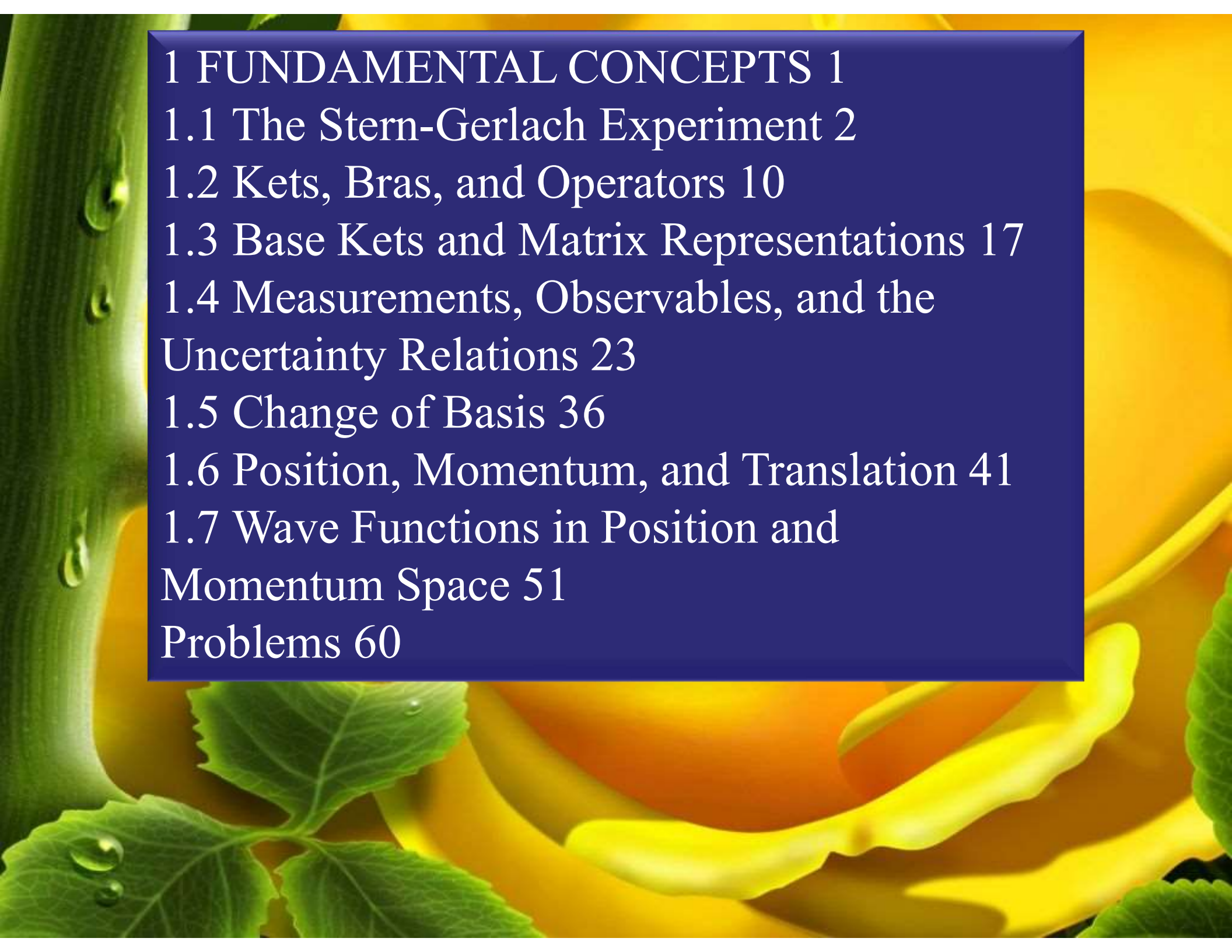
Modern Quantum Mechanics II

4) SYMMETRY IN QUANTUM MECHANICS

5) APPROXIMATION METHODS

6) IDENTICAL PARTICLES

7) SCATTERING THEORY



1 FUNDAMENTAL CONCEPTS 1

1.1 The Stern-Gerlach Experiment 2

1.2 Kets, Bras, and Operators 10

1.3 Base Kets and Matrix Representations 17

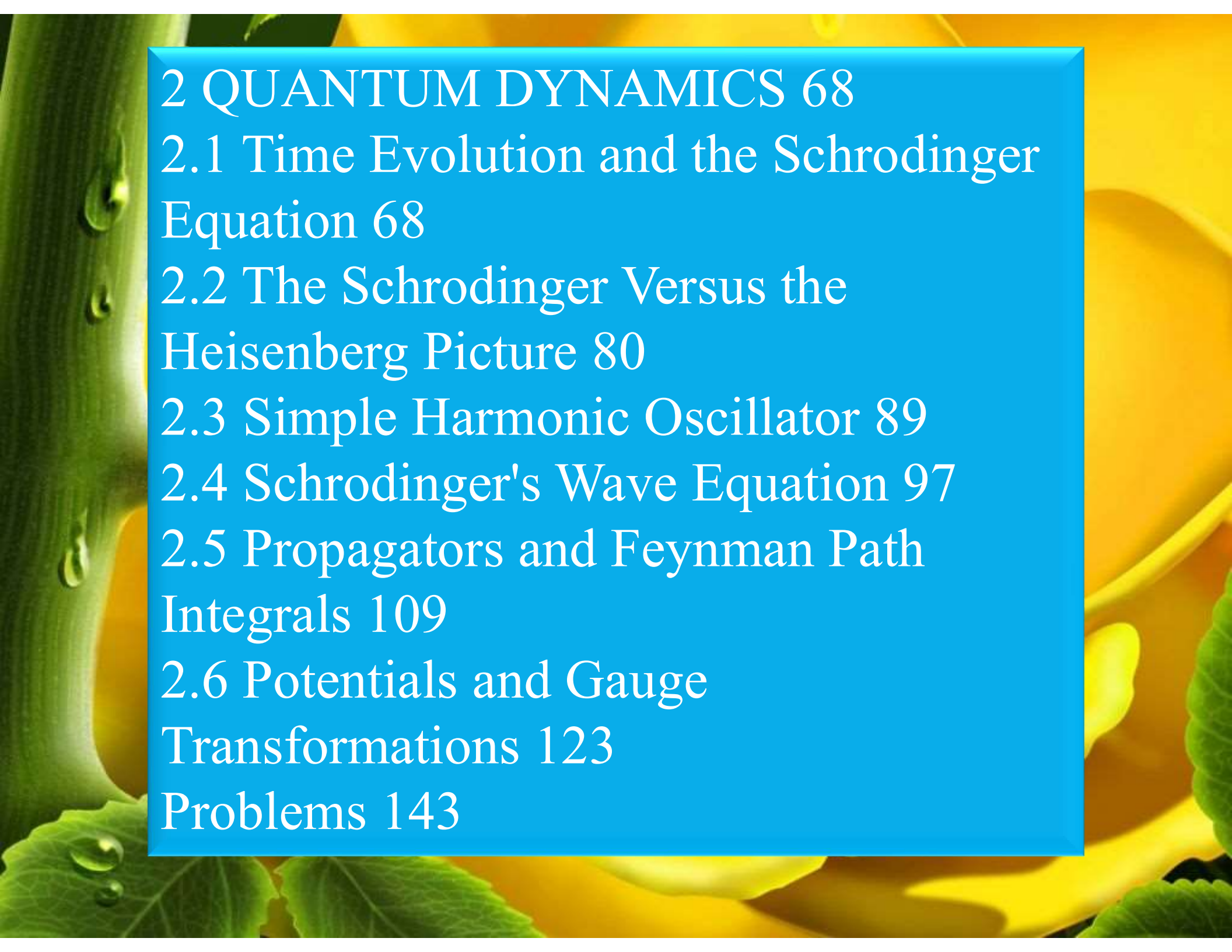
1.4 Measurements, Observables, and the
Uncertainty Relations 23

1.5 Change of Basis 36

1.6 Position, Momentum, and Translation 41

1.7 Wave Functions in Position and
Momentum Space 51

Problems 60



2 QUANTUM DYNAMICS 68

2.1 Time Evolution and the Schrodinger Equation 68

2.2 The Schrodinger Versus the Heisenberg Picture 80

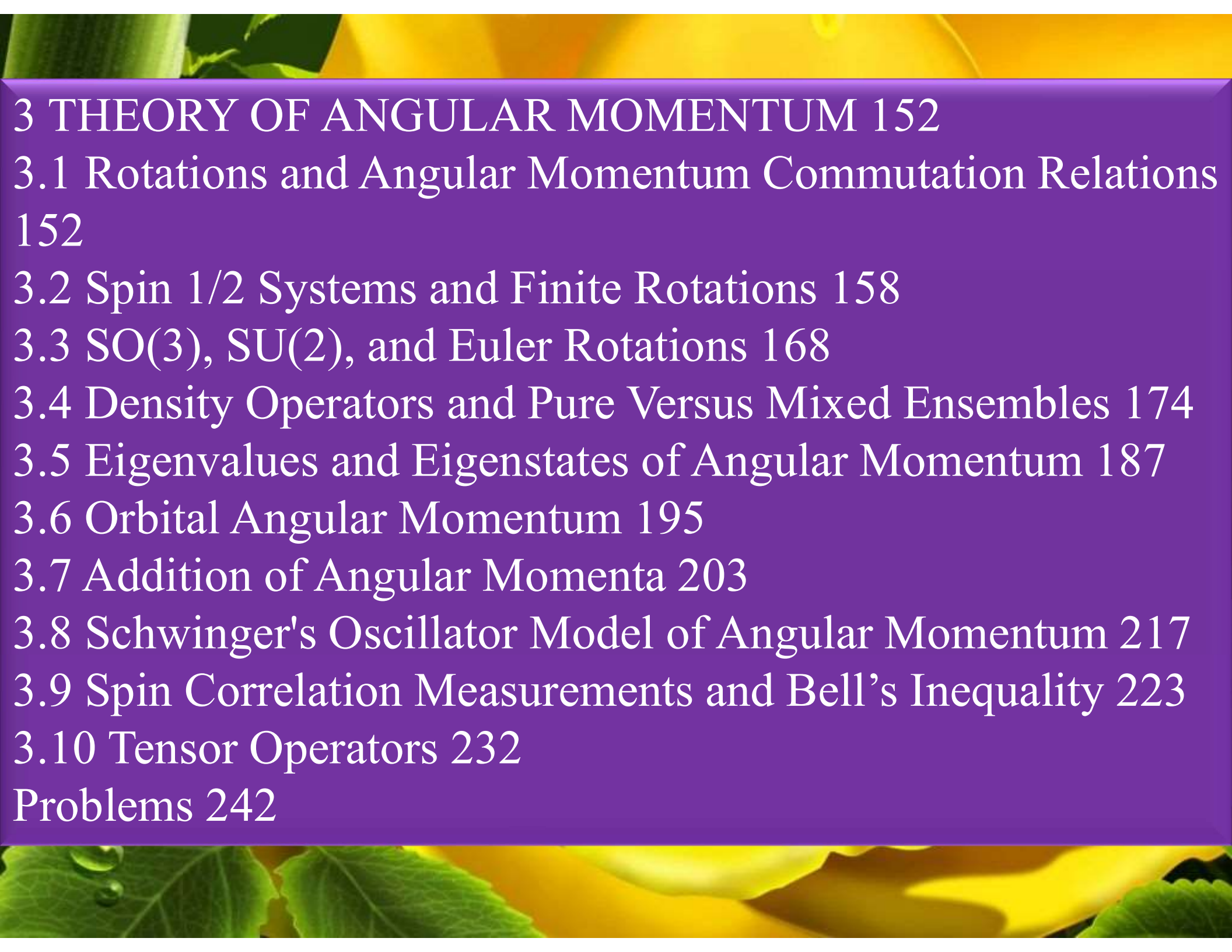
2.3 Simple Harmonic Oscillator 89

2.4 Schrodinger's Wave Equation 97

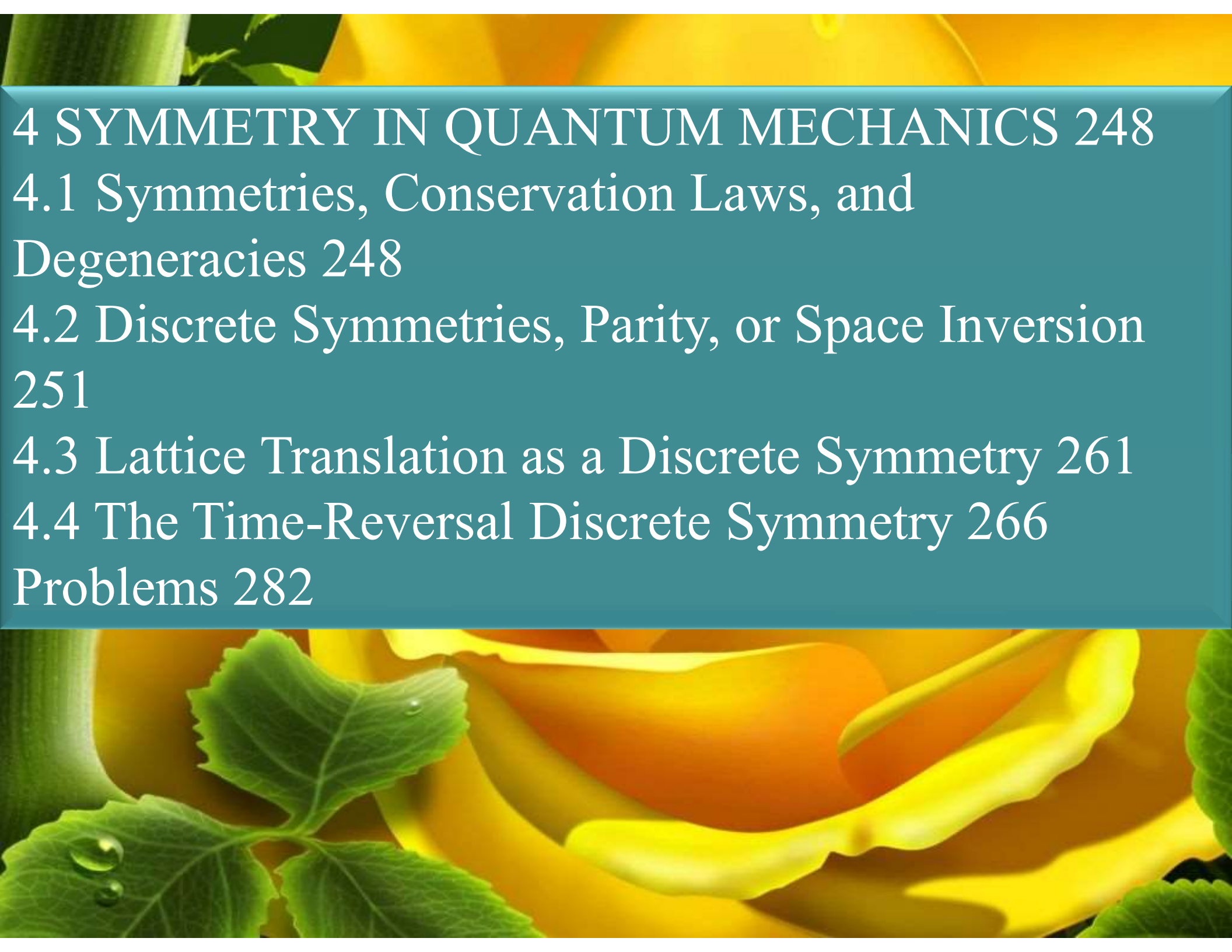
2.5 Propagators and Feynman Path Integrals 109

2.6 Potentials and Gauge Transformations 123

Problems 143



3	THEORY OF ANGULAR MOMENTUM	152
3.1	Rotations and Angular Momentum Commutation Relations	152
3.2	Spin 1/2 Systems and Finite Rotations	158
3.3	SO(3), SU(2), and Euler Rotations	168
3.4	Density Operators and Pure Versus Mixed Ensembles	174
3.5	Eigenvalues and Eigenstates of Angular Momentum	187
3.6	Orbital Angular Momentum	195
3.7	Addition of Angular Momenta	203
3.8	Schwinger's Oscillator Model of Angular Momentum	217
3.9	Spin Correlation Measurements and Bell's Inequality	223
3.10	Tensor Operators	232
	Problems	242



4 SYMMETRY IN QUANTUM MECHANICS 248

4.1 Symmetries, Conservation Laws, and Degeneracies 248

4.2 Discrete Symmetries, Parity, or Space Inversion 251

4.3 Lattice Translation as a Discrete Symmetry 261

4.4 The Time-Reversal Discrete Symmetry 266

Problems 282

5 APPROXIMATION METHODS 285

5.1 Time-Independent Perturbation Theory:
Nondegenerate Case 285

5.2 Time-Independent Perturbation Theory:
The Degenerate Case 298

5.3 Hydrogenlike Atoms: Fine Structure and the Zeeman
Effect 304

5.4 Variational Methods 313

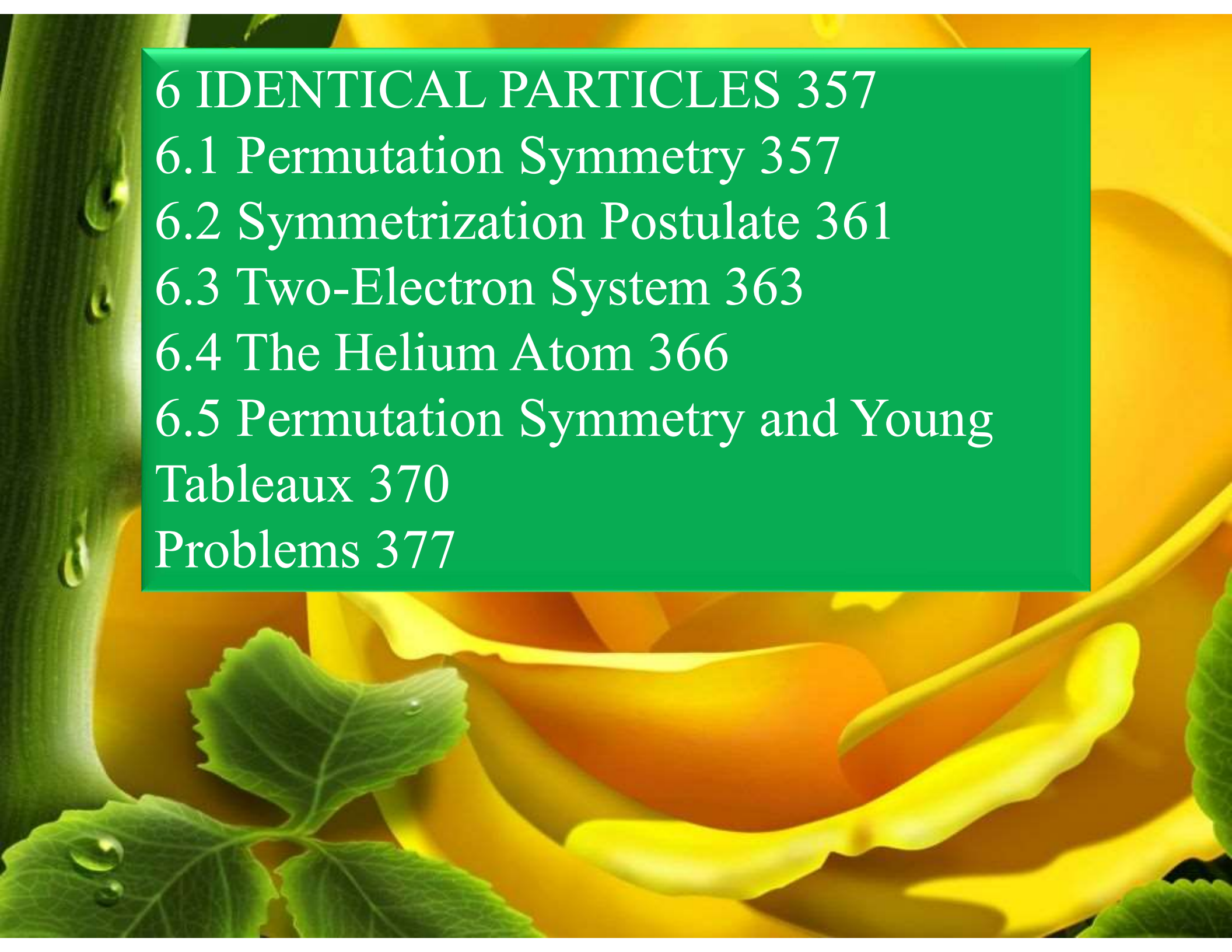
5.5 Time-Dependent Potentials: The Interaction Picture 316

5.6 Time-Dependent Perturbation Theory 325

5.7 Applications to Interactions with the Classical
Radiation Field 335

5.8 Energy Shift and Decay Width 341

Problems 345



6 IDENTICAL PARTICLES 357

6.1 Permutation Symmetry 357

6.2 Symmetrization Postulate 361

6.3 Two-Electron System 363

6.4 The Helium Atom 366

6.5 Permutation Symmetry and Young
Tableaux 370

Problems 377

7	SCATTERING THEORY	379
7.1	The Lippmann-Schwinger Equation	379
7.2	The Born Approximation	386
7.3	Optical Theorem	390
7.4	Eikonal Approximation	392
7.5	Free-Particle States: Plane Waves Versus Spherical Waves	395
7.6	Method of Partial Waves	399
7.7	Low-Energy Scattering and Bound States	410
7.8	Resonance Scattering	418
7.9	Identical Particles and Scattering	421
7.10	Symmetry Considerations in Scattering	422
7.11	Time-Dependent Formulation of Scattering	424
7.12	Inelastic Electron-Atom Scattering	429
7.13	Coulomb Scattering	434
	Problems	441